

ESCI7205: HW 7

Due: Tue Nov. 10, 2009

1) This is a short exercise for Matlab. Calculate and plot the acceleration of gravity, $g(r)$, from $r=0$ to $r=4R_e$, for a planet that consists of a core and mantle (use radii of $R_c = 3480$ km for the core and $R_p = 6371$ km for the planet, and densities of 11.5 g/cm^3 for the core and 5 g/cm^3 for the mantle). Compare the qualitative results from this planet to $g(r)$ for earth.

Useful information: $G = 6.6726 \cdot 10^{-11} \text{ Nm}^2\text{kg}^{-2}$.

Acceleration of gravity as a function of radius inside a sphere of uniform density ρ :

$$g(r) = \frac{GM(r)}{r^2} = \frac{G\left(\frac{4}{3}\pi r^3 \rho\right)}{r^2} = \frac{4}{3}\pi G \rho r .$$

Acceleration of gravity as a function of distance outside a sphere of uniform density:

$$g(r) = MGr^{-2} .$$

$M(r)$ and M are the masses as a function of radius when inside and the total mass when outside.

The volume of a sphere is $V = \frac{4}{3}\pi r^3$.

Ave dens whole earth 5.5 g/cm^3 .