

# Earth Science Applications of Space Based Geodesy

DES-7355

Tu-Th

9:40-11:05

Seminar Room in 3892 Central Ave. (Long building)

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Office: 3892 Central Ave, Room 103

678-4929

Office Hours – Wed 14:00-16:00 or if I'm in my office.

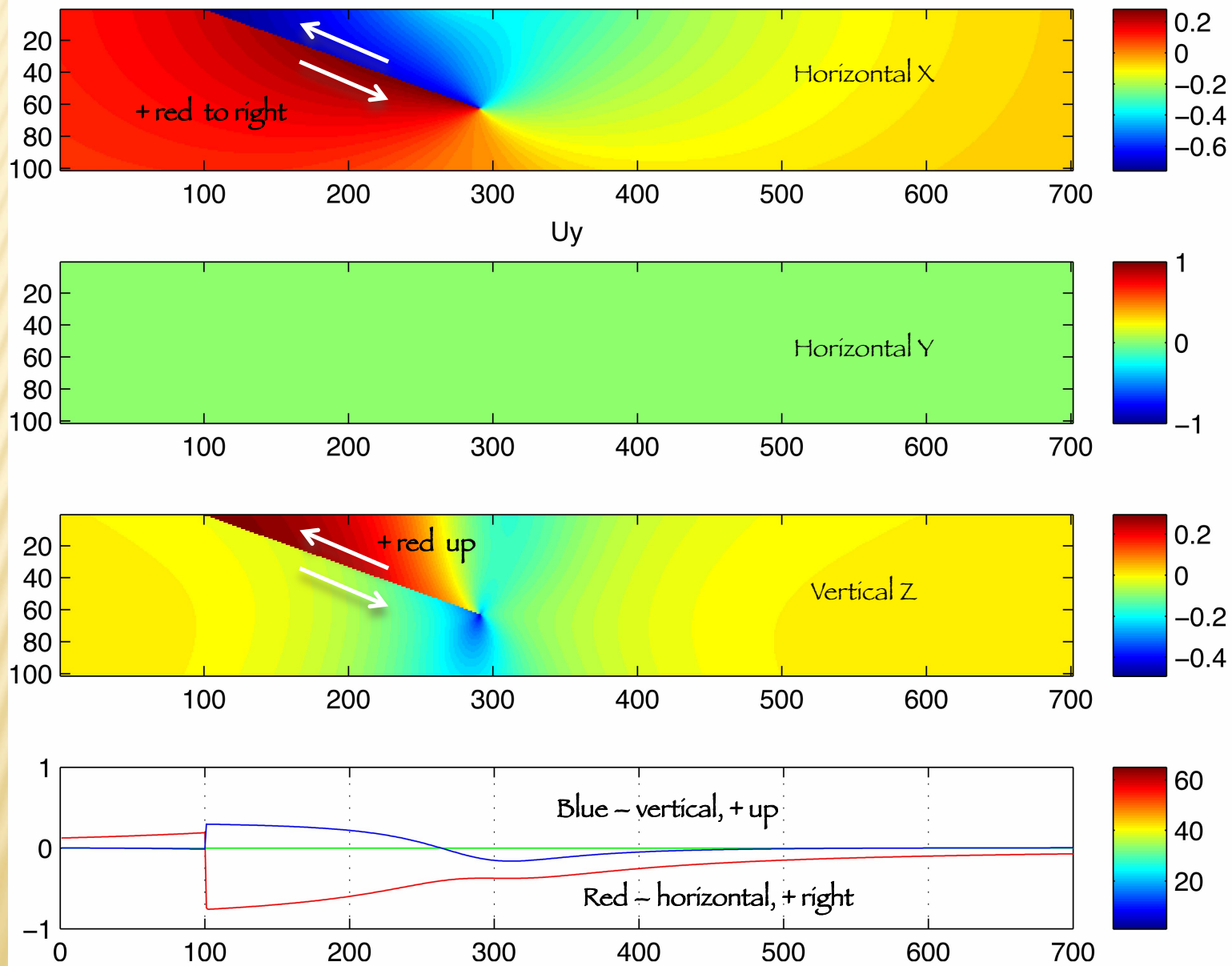
[http://www.ceri.memphis.edu/people/smalley/ESCI7355/ESCI\\_7355\\_Applications\\_of\\_Space\\_Based\\_Geodesy.html](http://www.ceri.memphis.edu/people/smalley/ESCI7355/ESCI_7355_Applications_of_Space_Based_Geodesy.html)

Class 21

Interplate thrust faulting.

Co-seismic

# Co-seismic, no tectonics



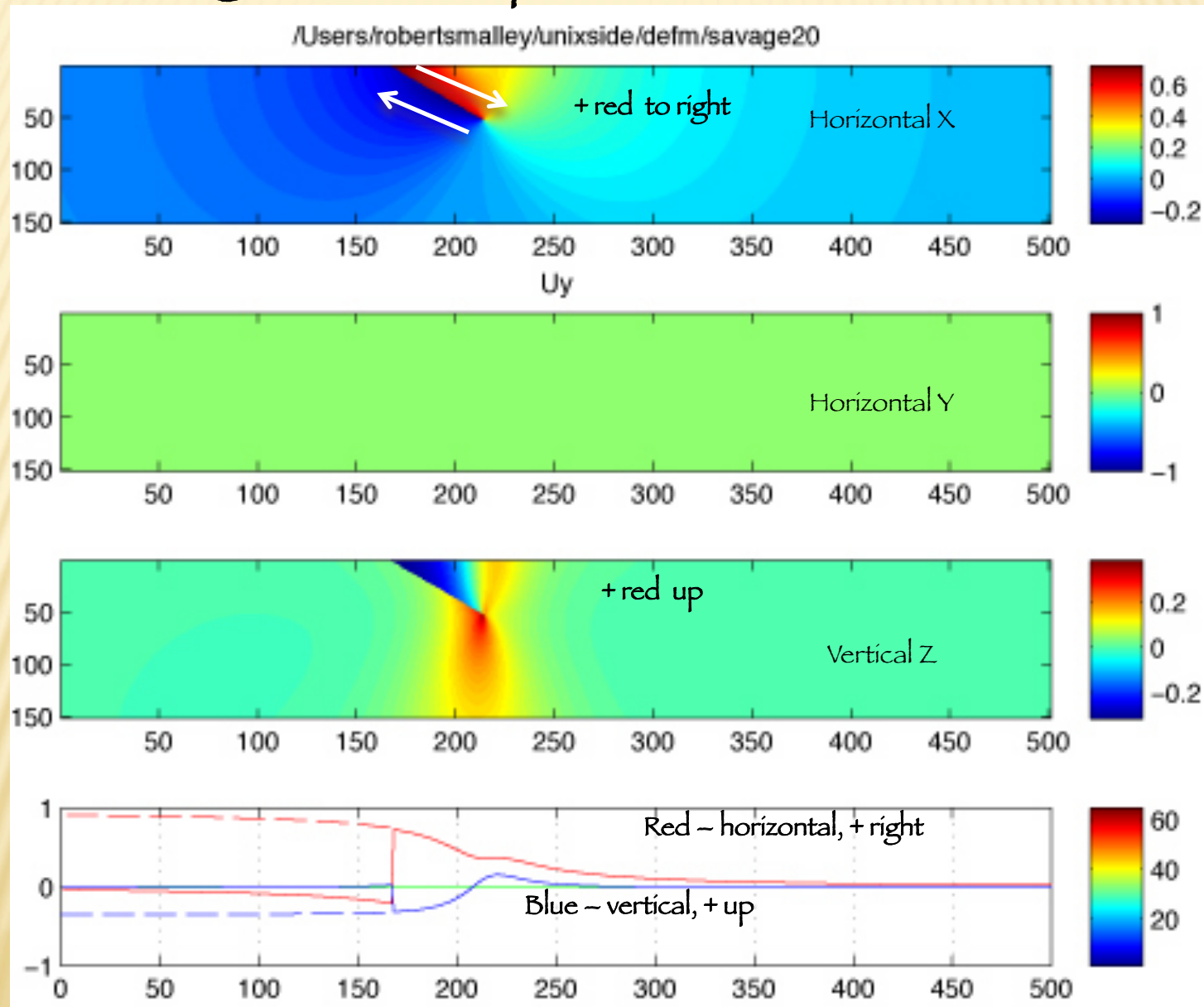


Interplate interseismic.

Two ways

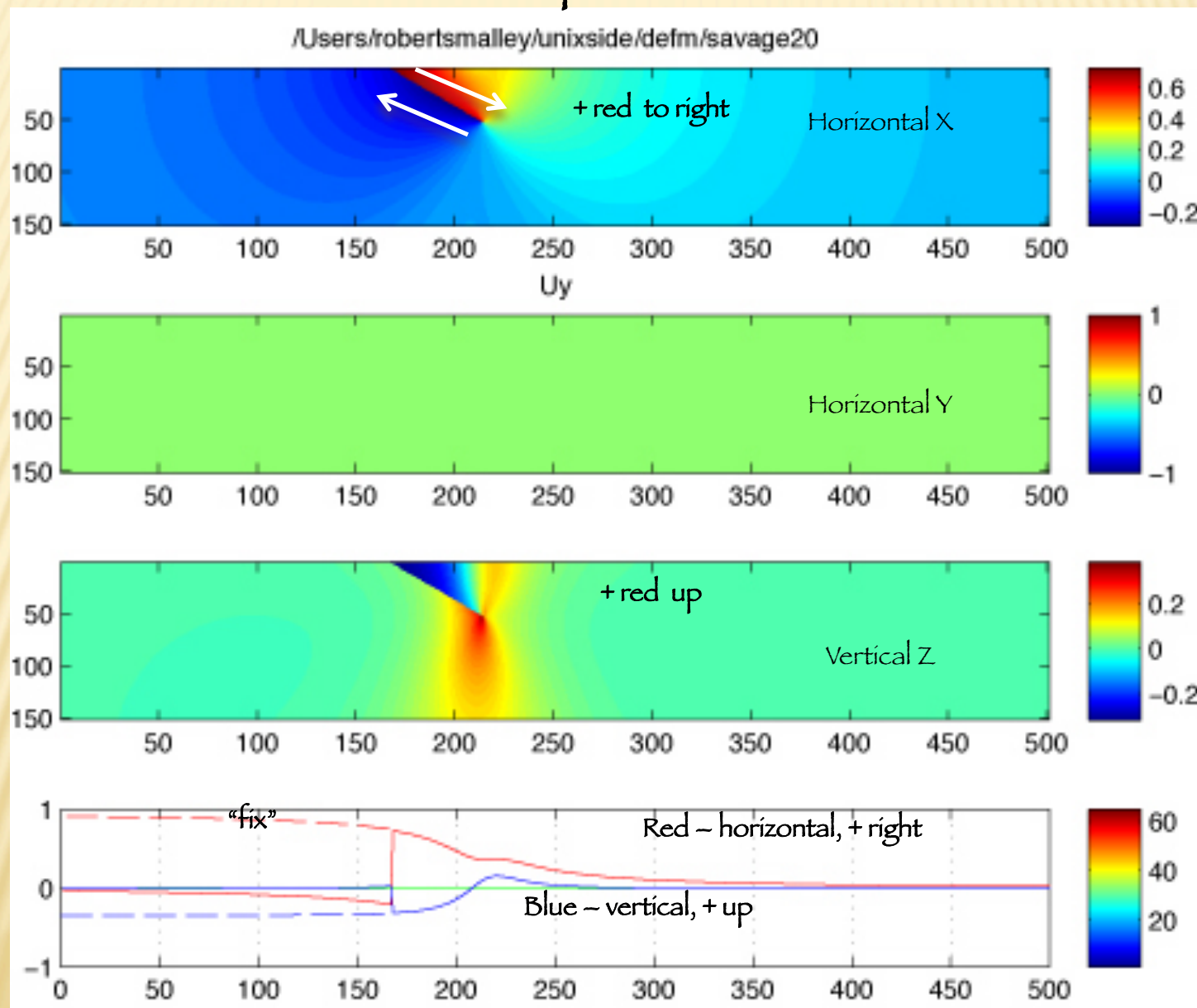


# Savage back-slip model for interseismic



Tectonic + Elastic perturbation

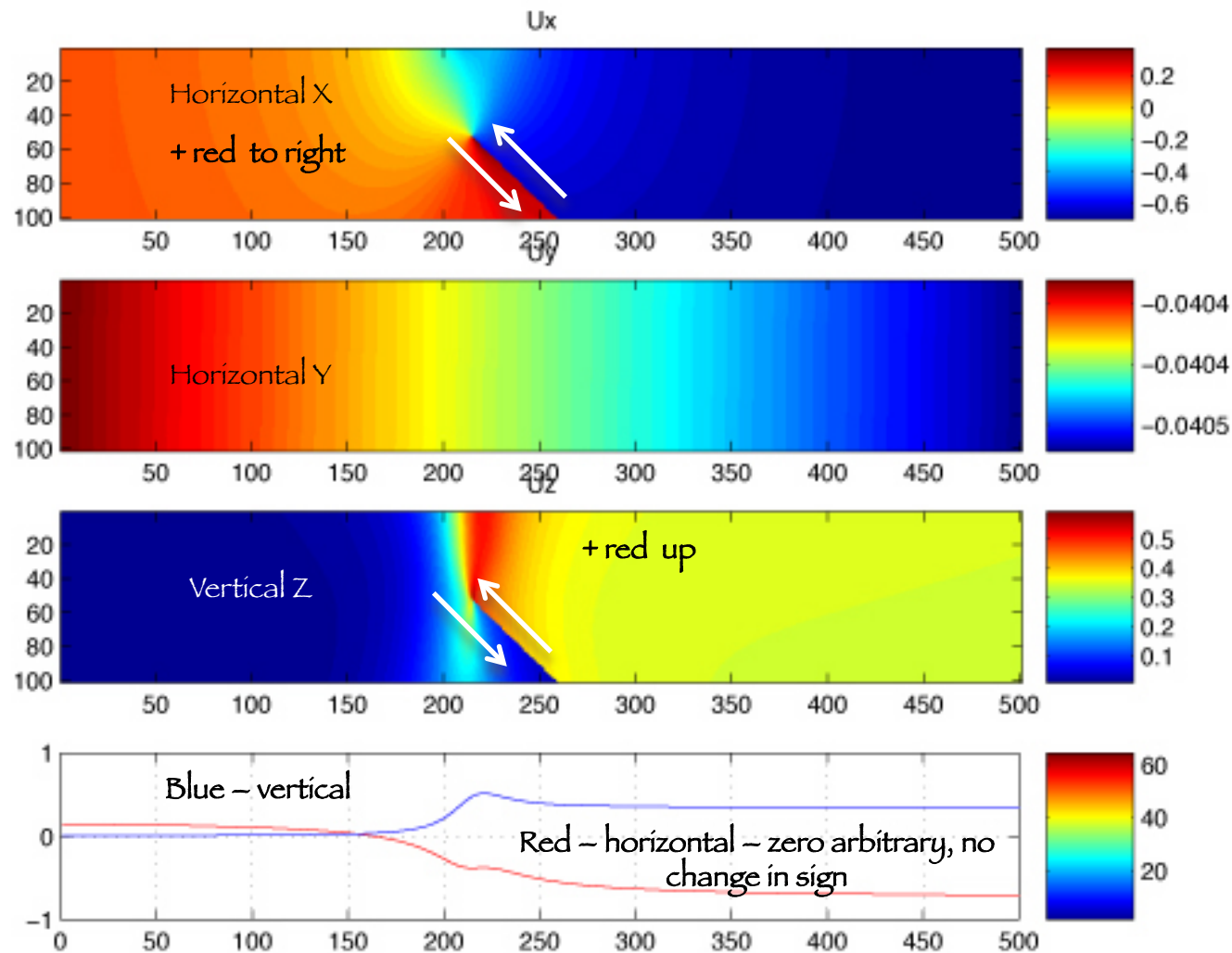
# Run the earthquake “backwards”



Tectonic + Elastic perturbation (works for horizontal, not vertical)

# Down-dip slip model for interseismic

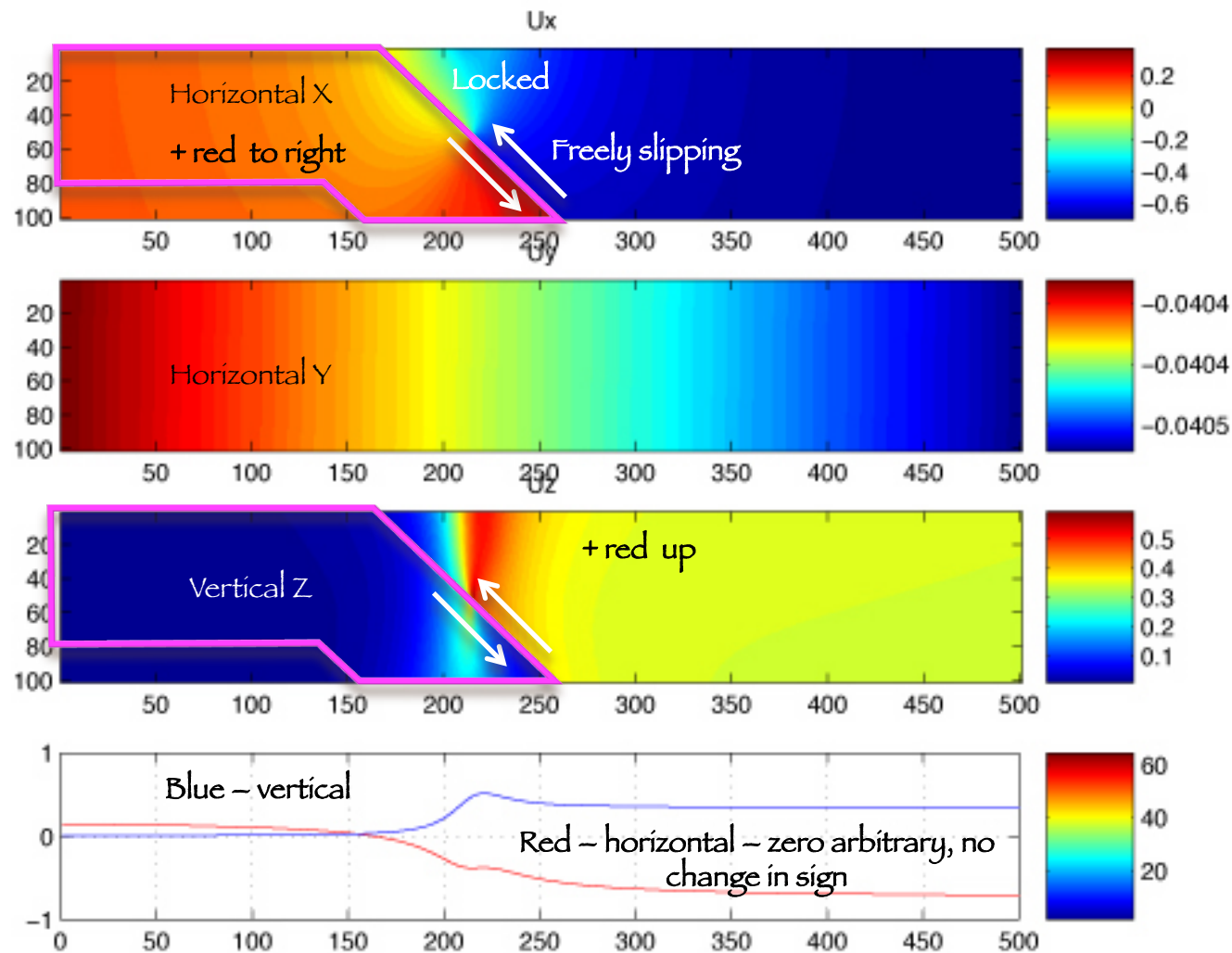
(does not have name)

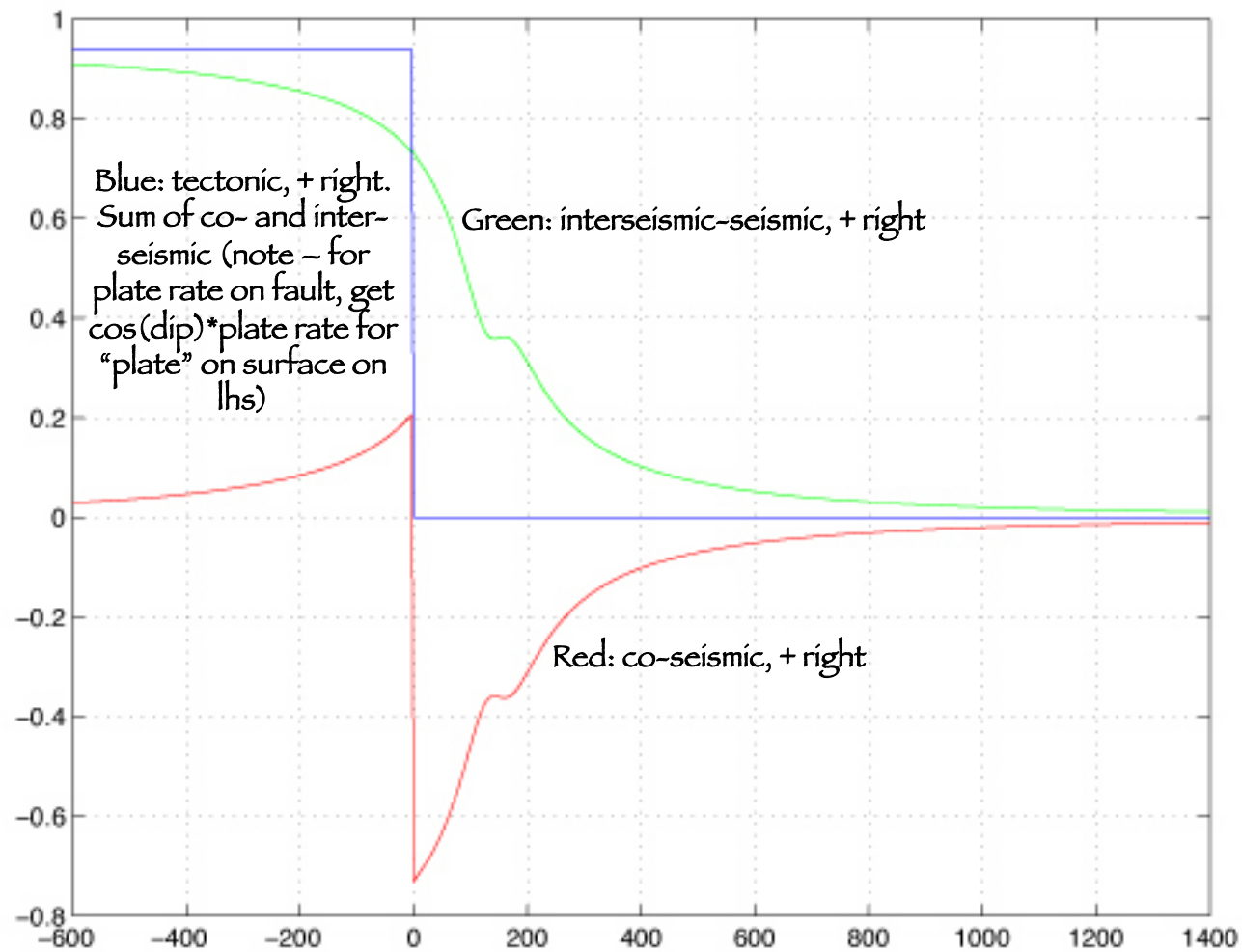




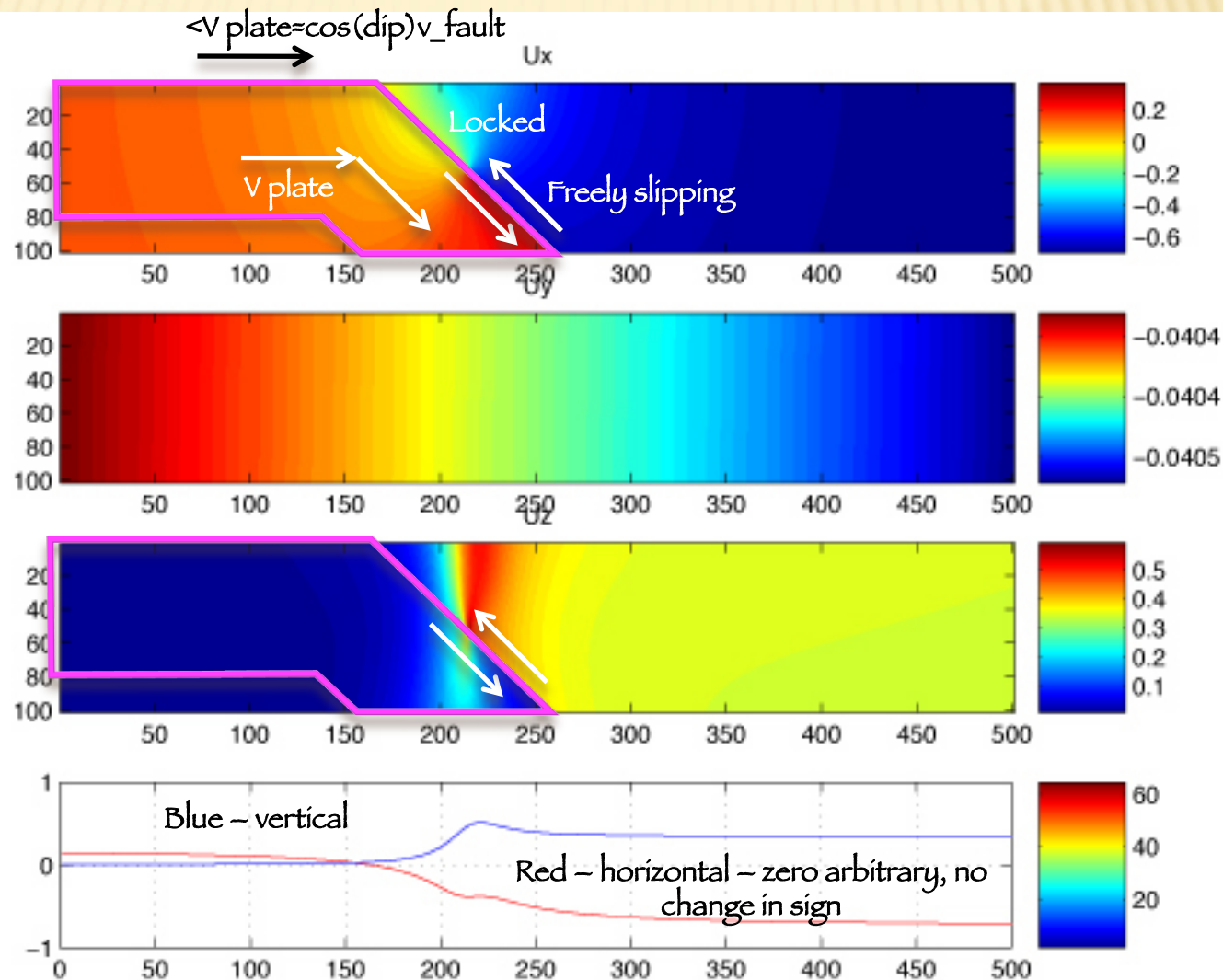
# Down-dip slip model for interseismic

(based on idea of subducting plate continuing)



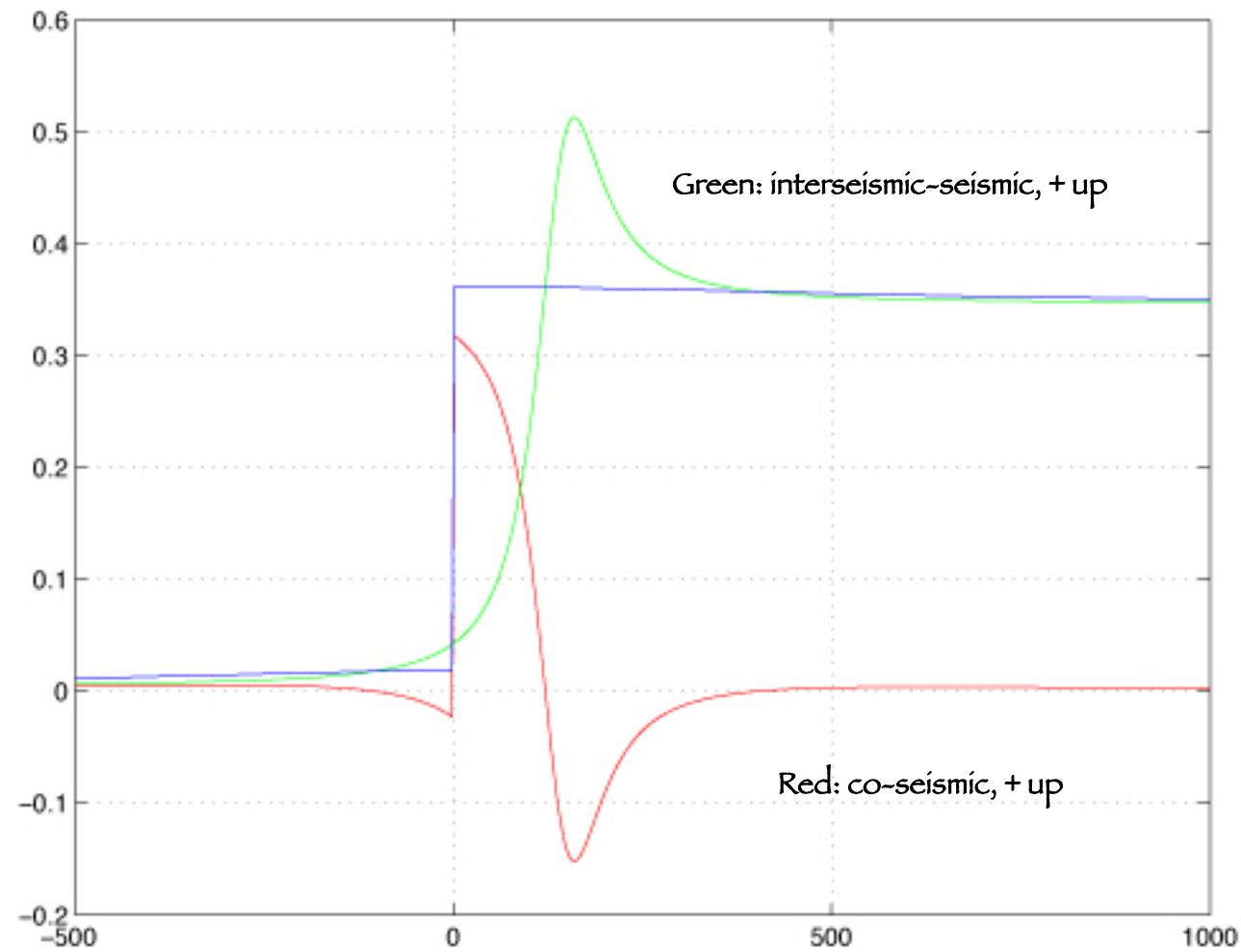


Relative velocity across fault – broken into horizontal and vertical components, so don't get v-plate along surface (the desired physics), get horizontal component.

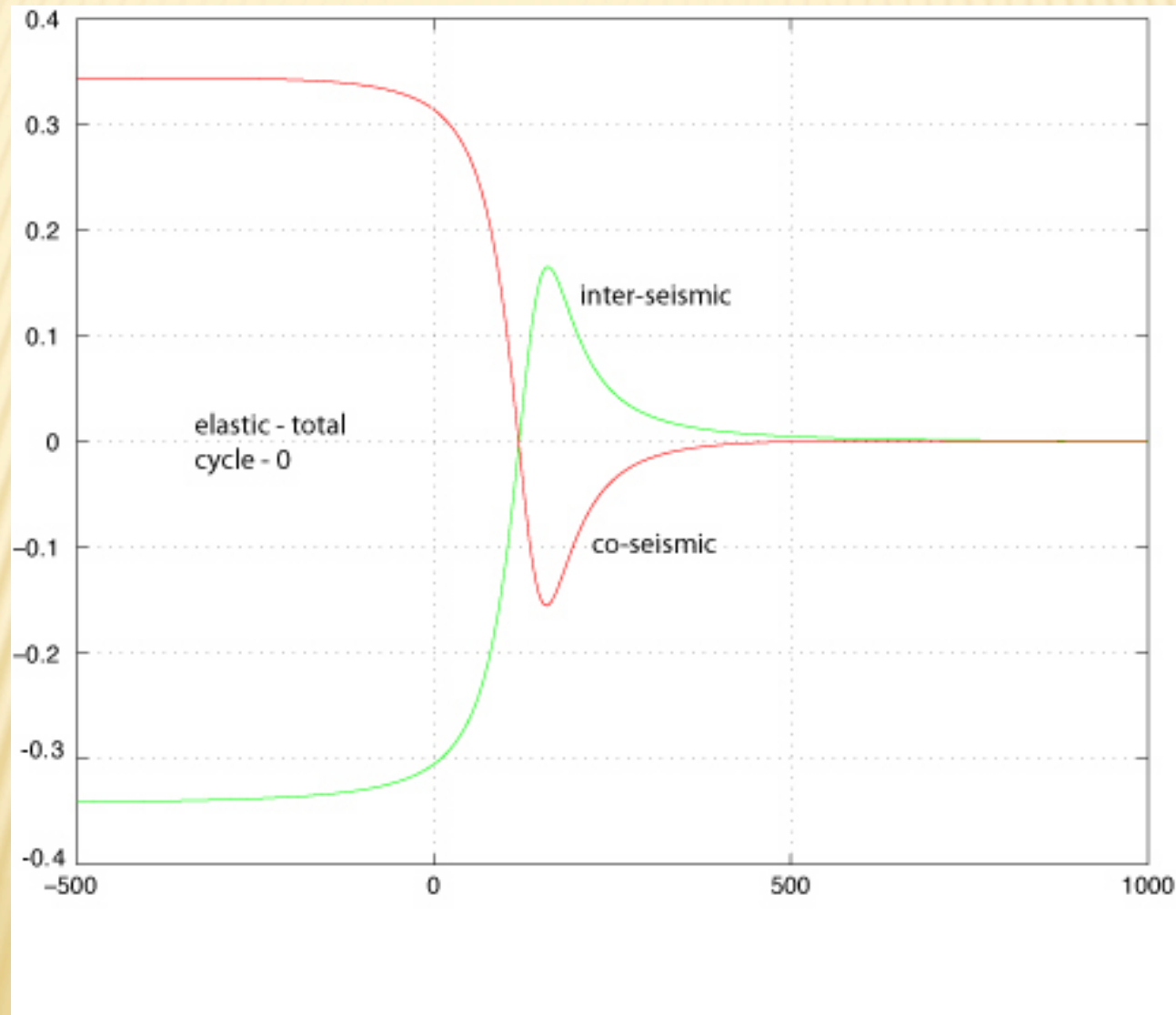




## Vertical – inter-seismic and co-seismic

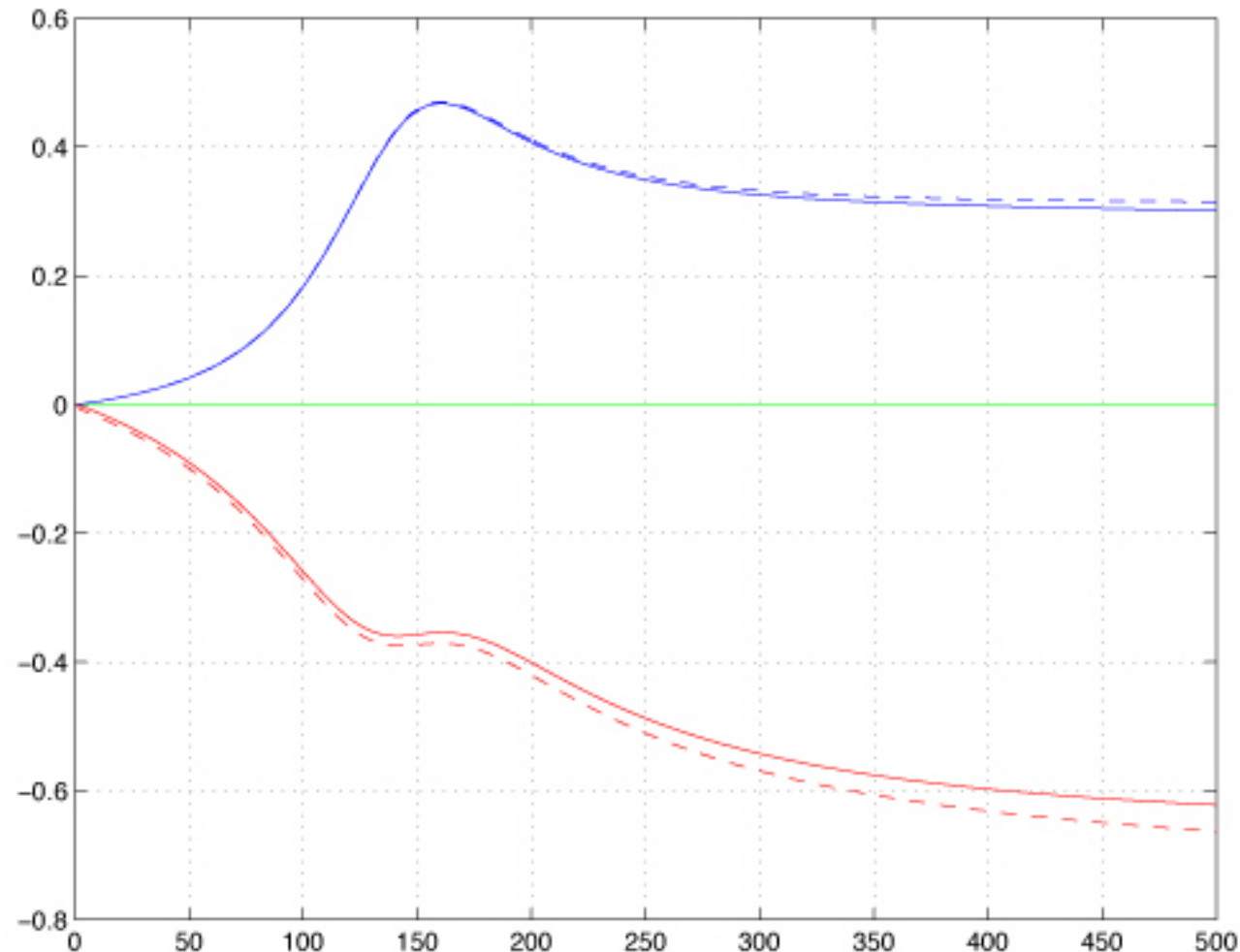


Vertical – inter-seismic and co-seismic, total cycle wrt far field upper plate.



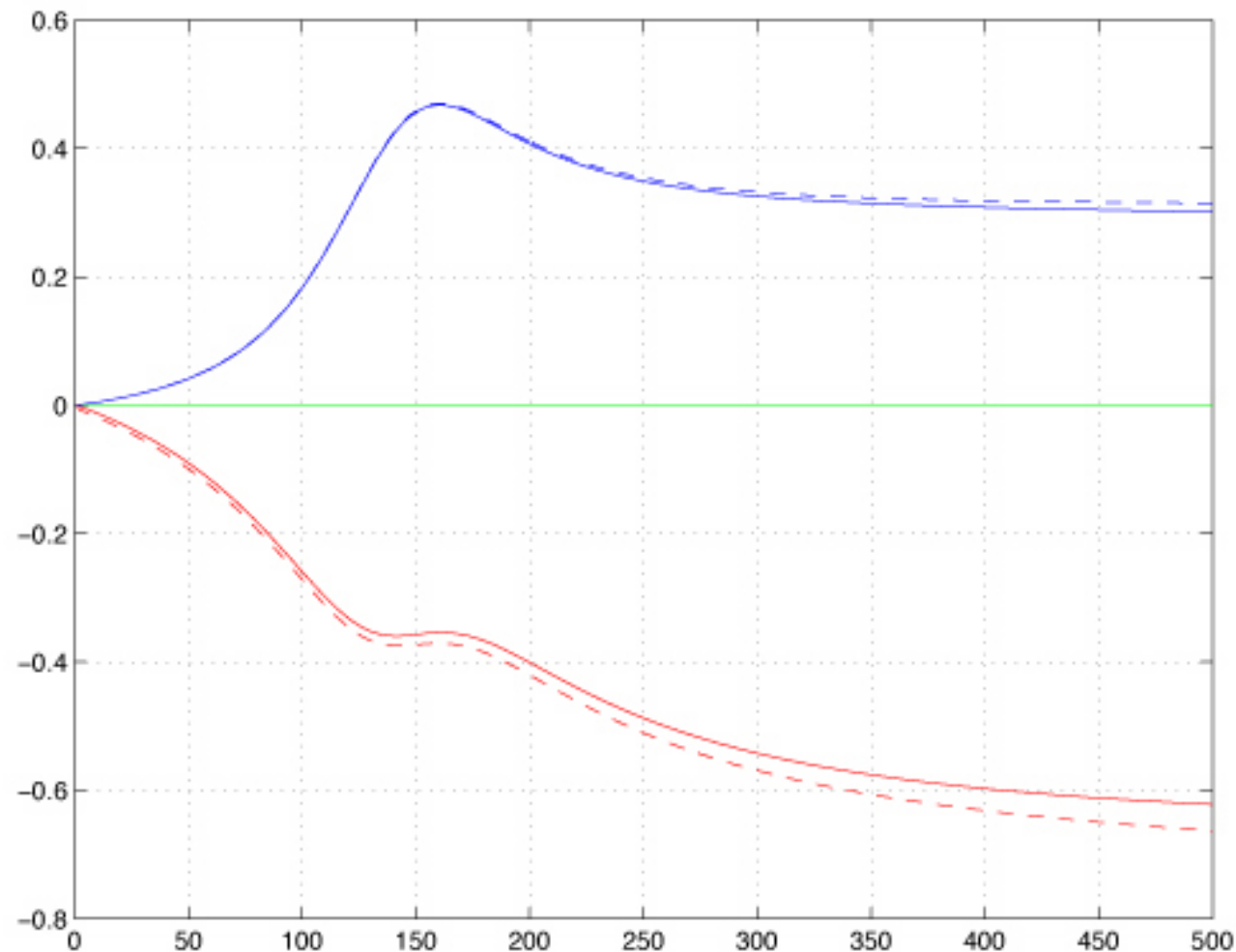
# Compare Savage back-slip & down-dip extension model

## Basically the same

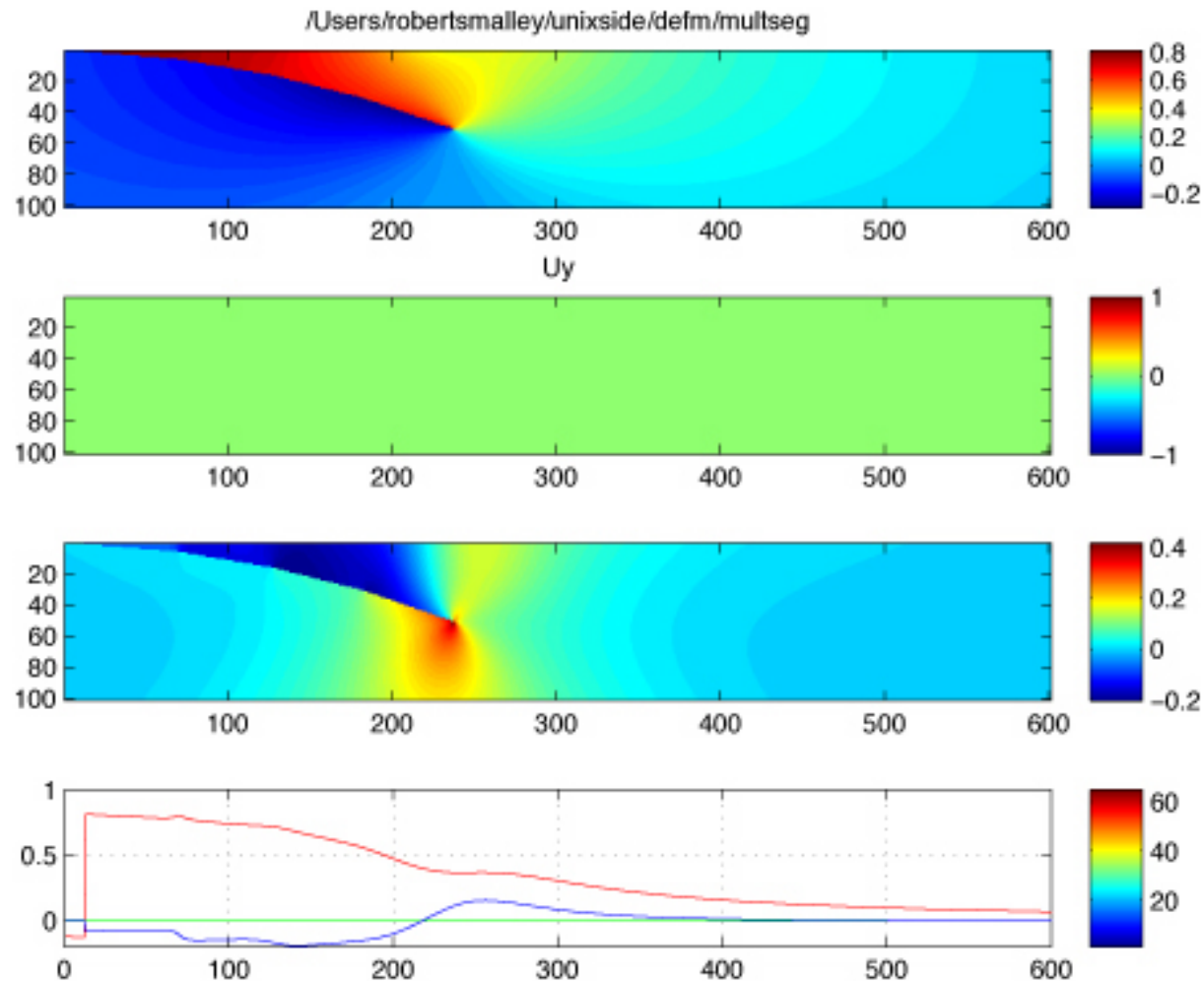




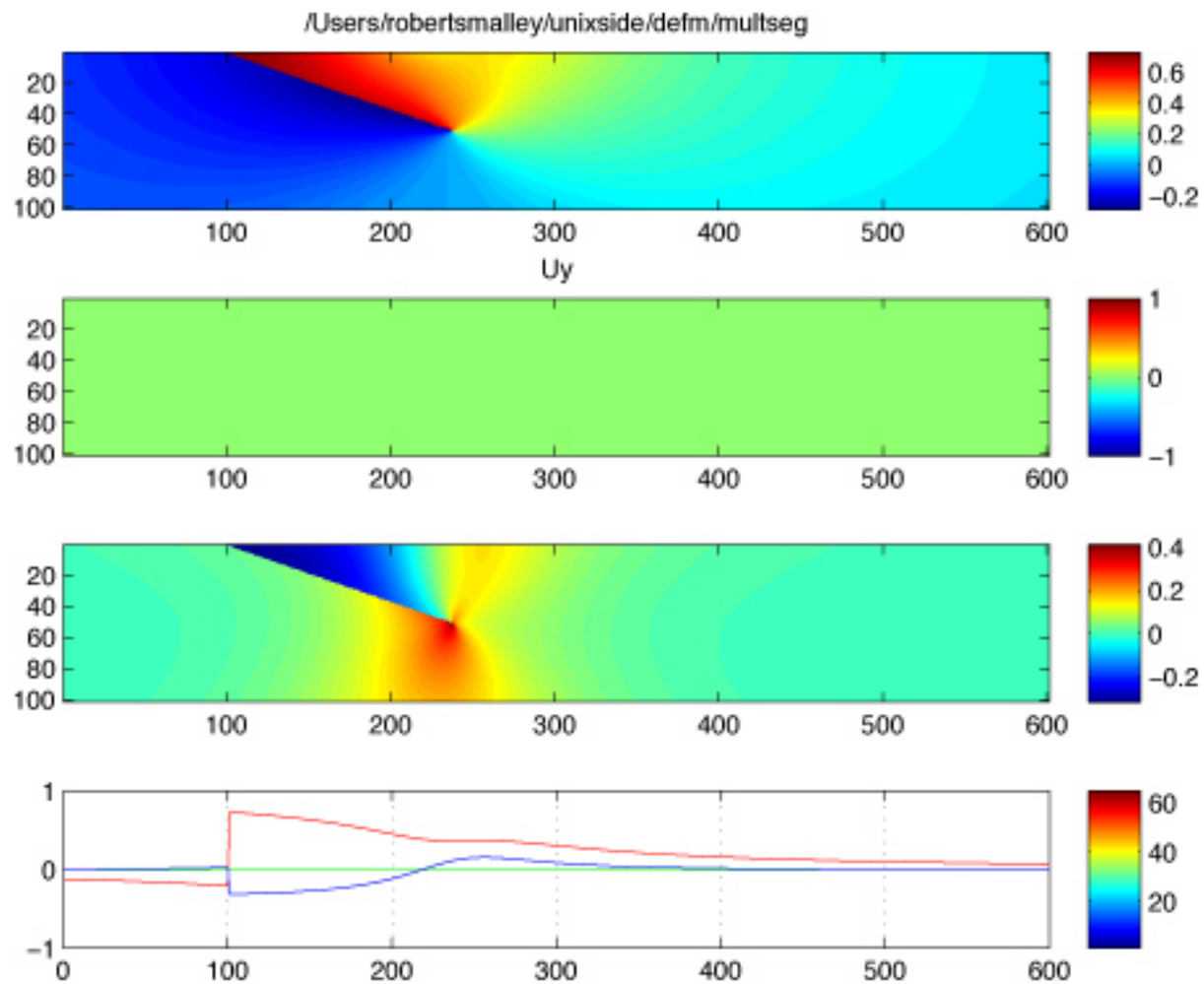
Horizontal has tectonics without “fix” (but at  $\cos$  of dip angle), but vertical has whole half of medium on hanging wall side going up (at  $\sin$  of dip angle)



# Popular variations – multi-segment interplate interface

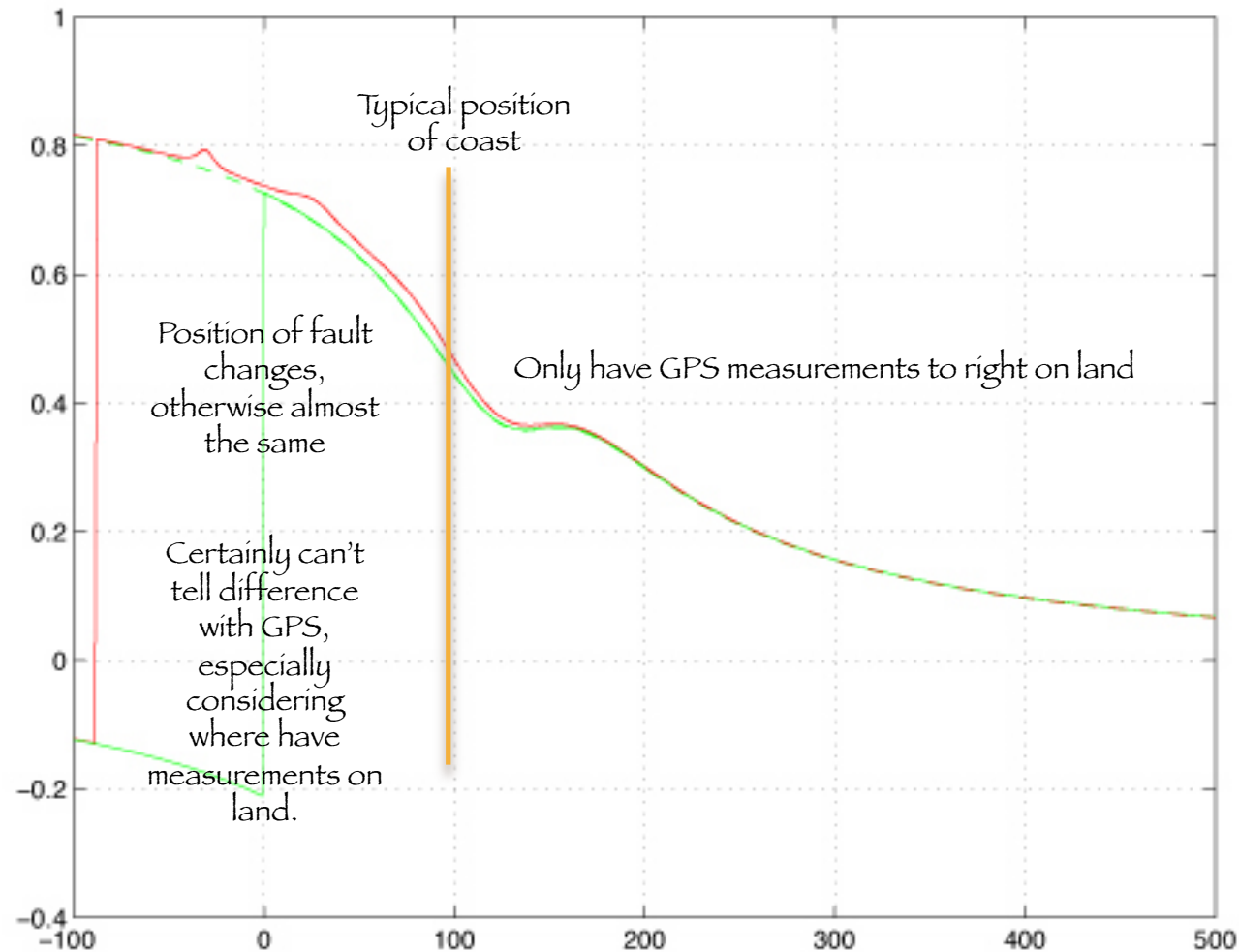


# Compare to single-segment interplate interface

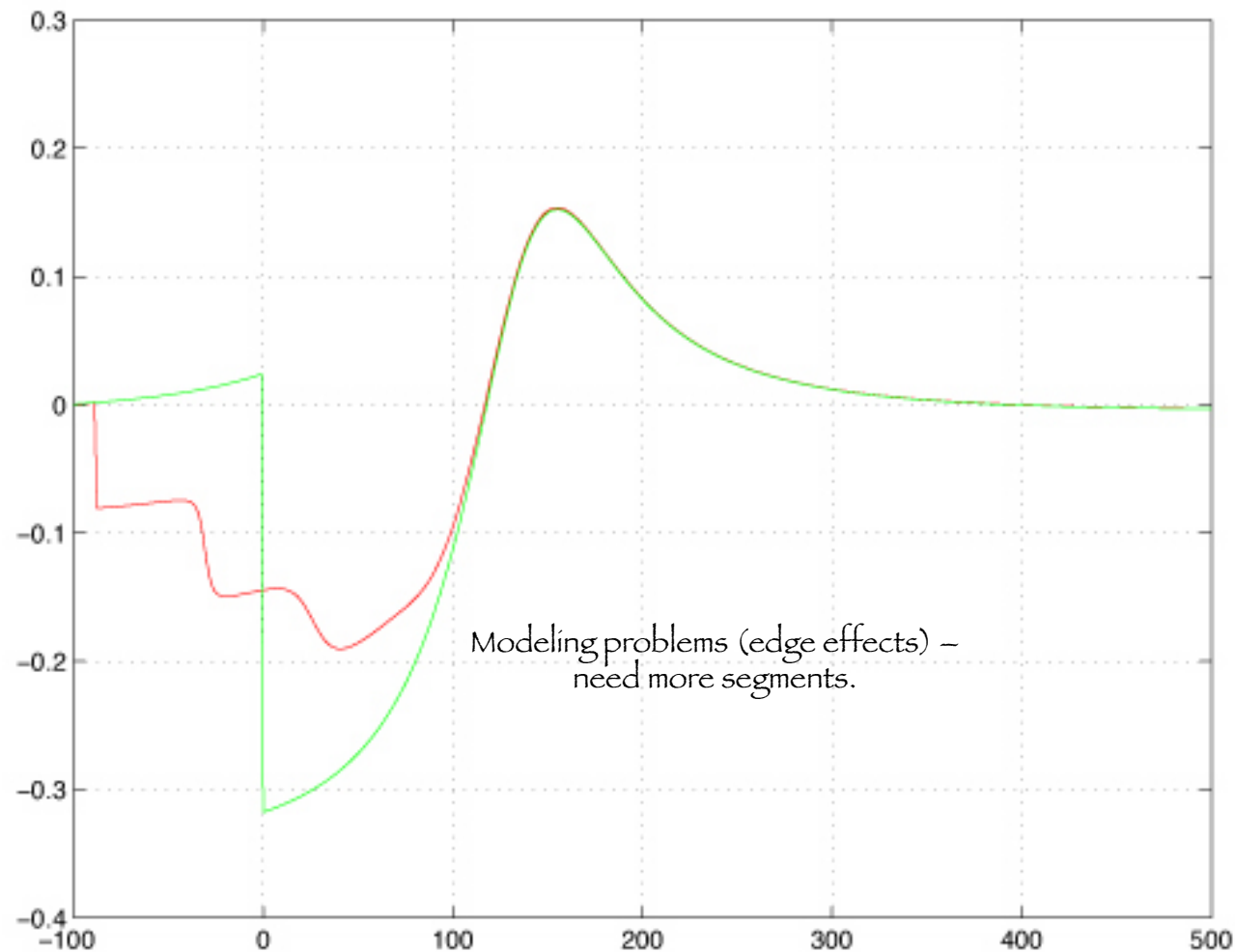




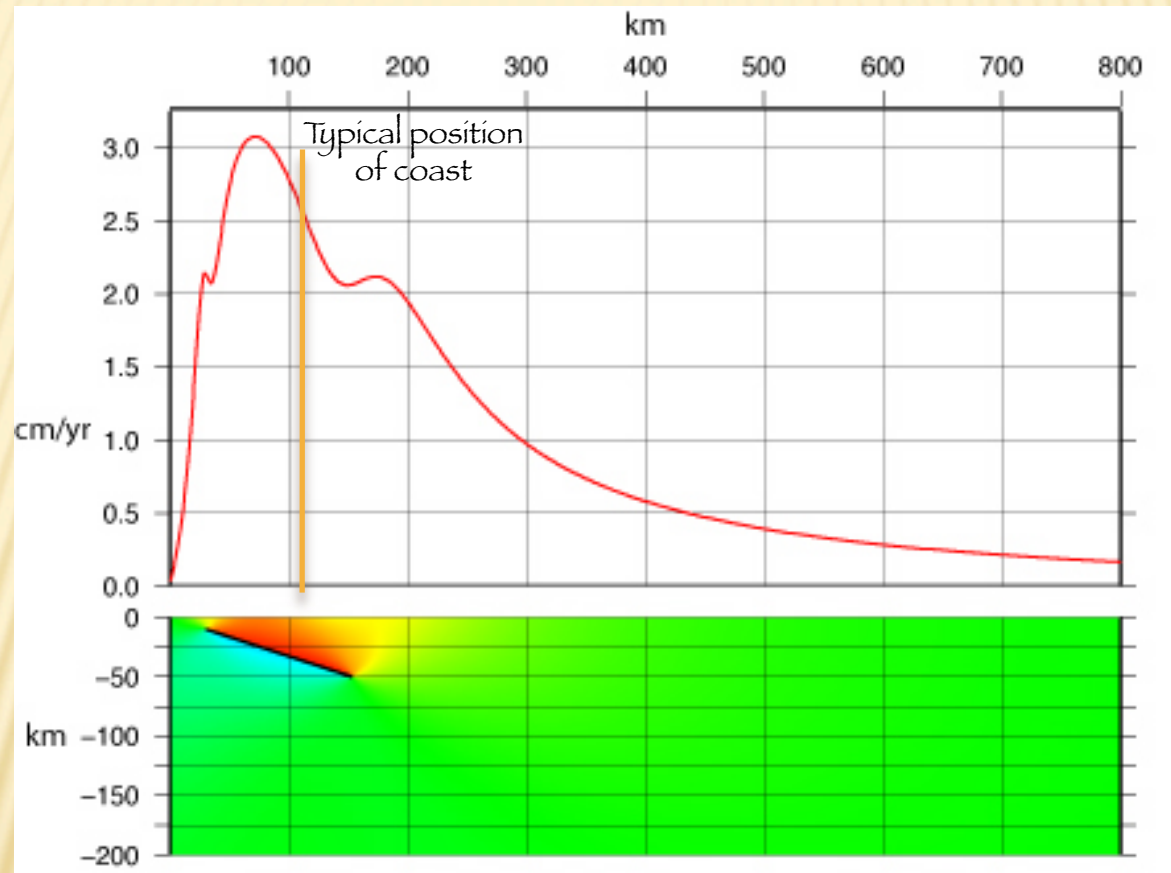
# Compare single-, multi-segment horizontal



# Compare single-, multi-segment Vertical

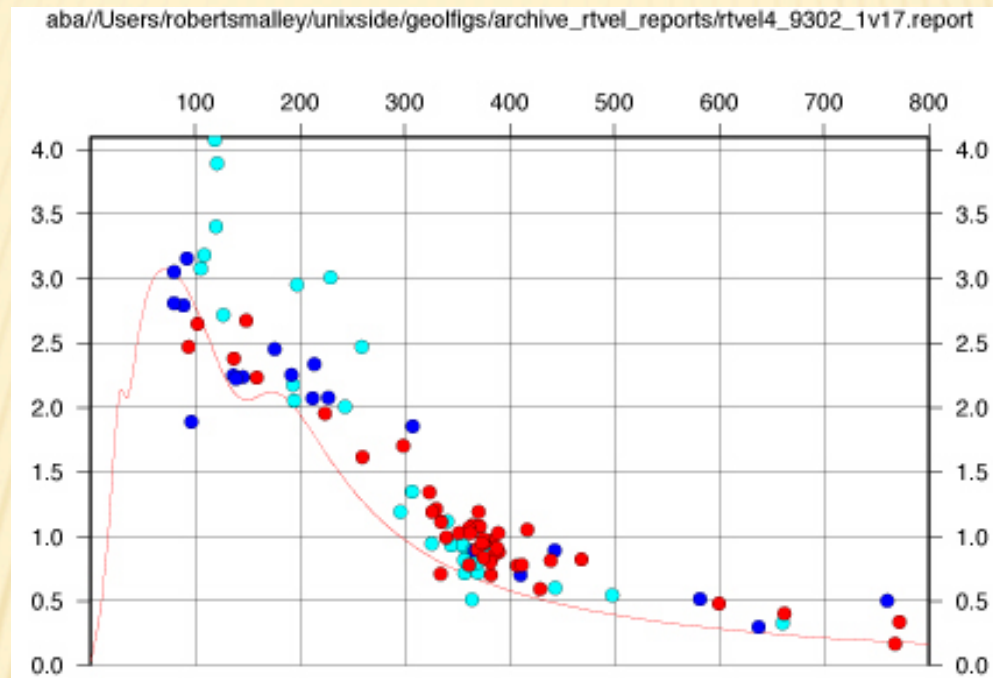


# Popular variations – fault does not outcrop (locked at top)

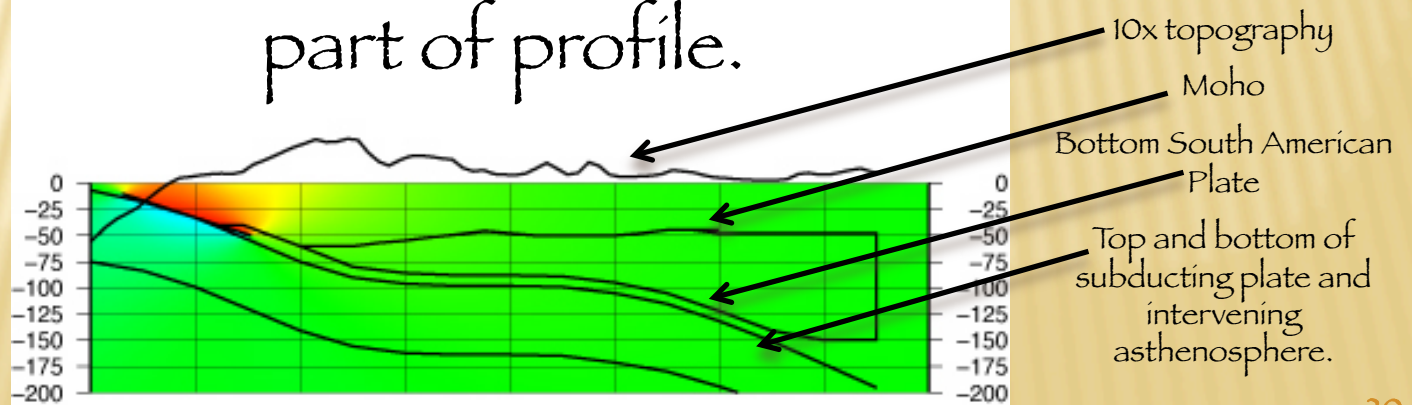


Geology, geophysics modeling support this, geodesy  
can't see it.

# Going overboard

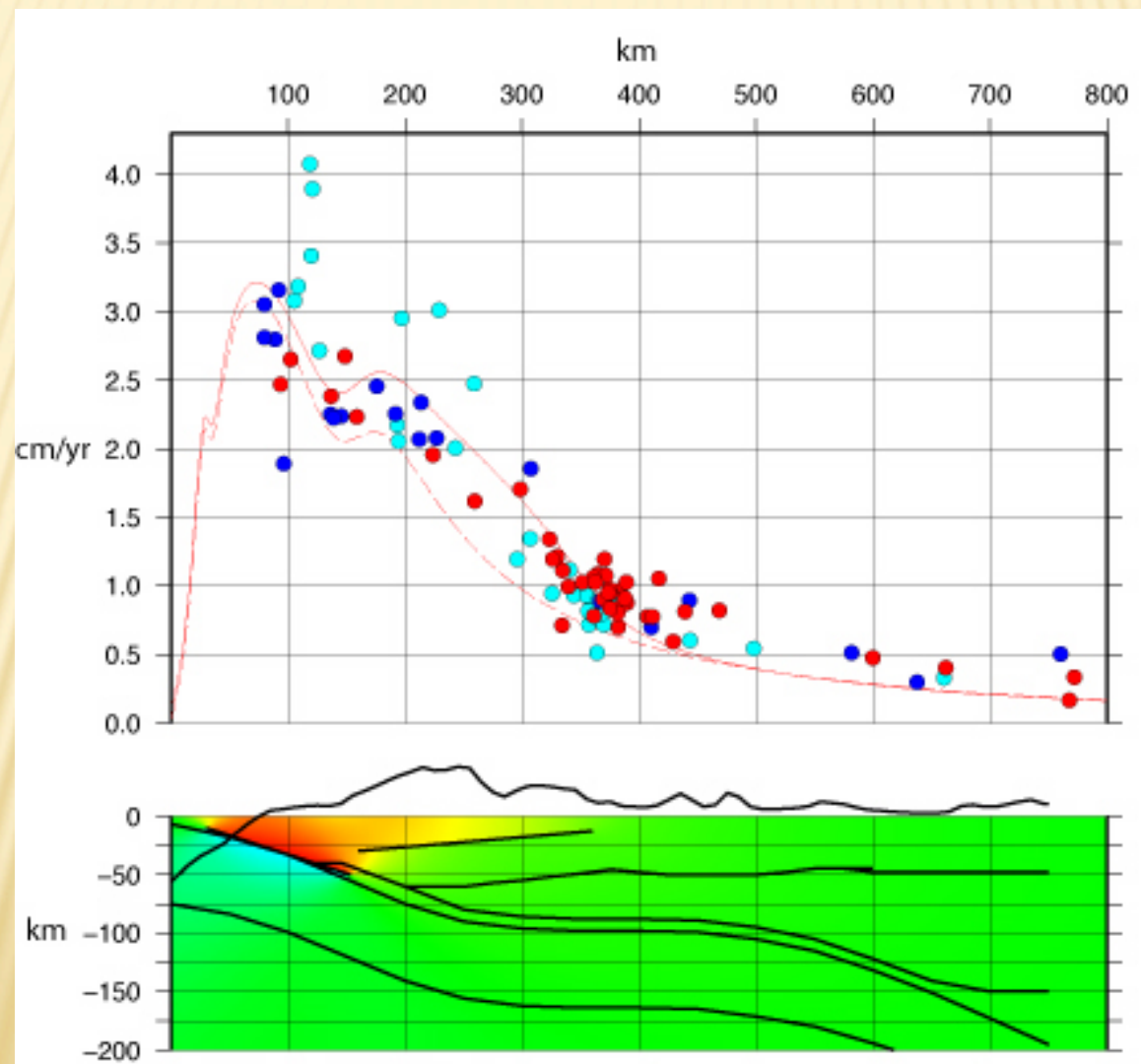


Single locked fault, does not match GPS data in central part of profile.

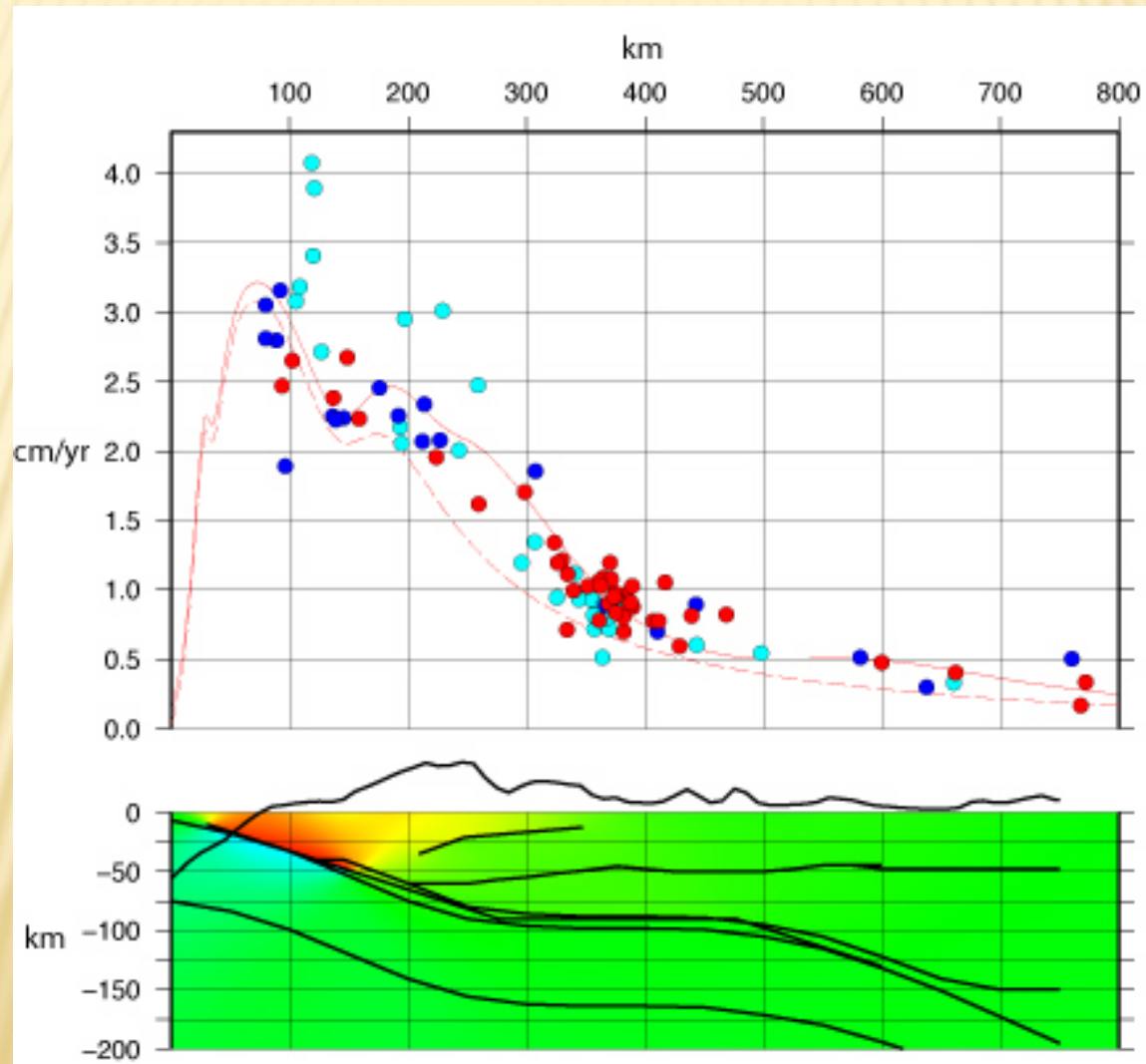




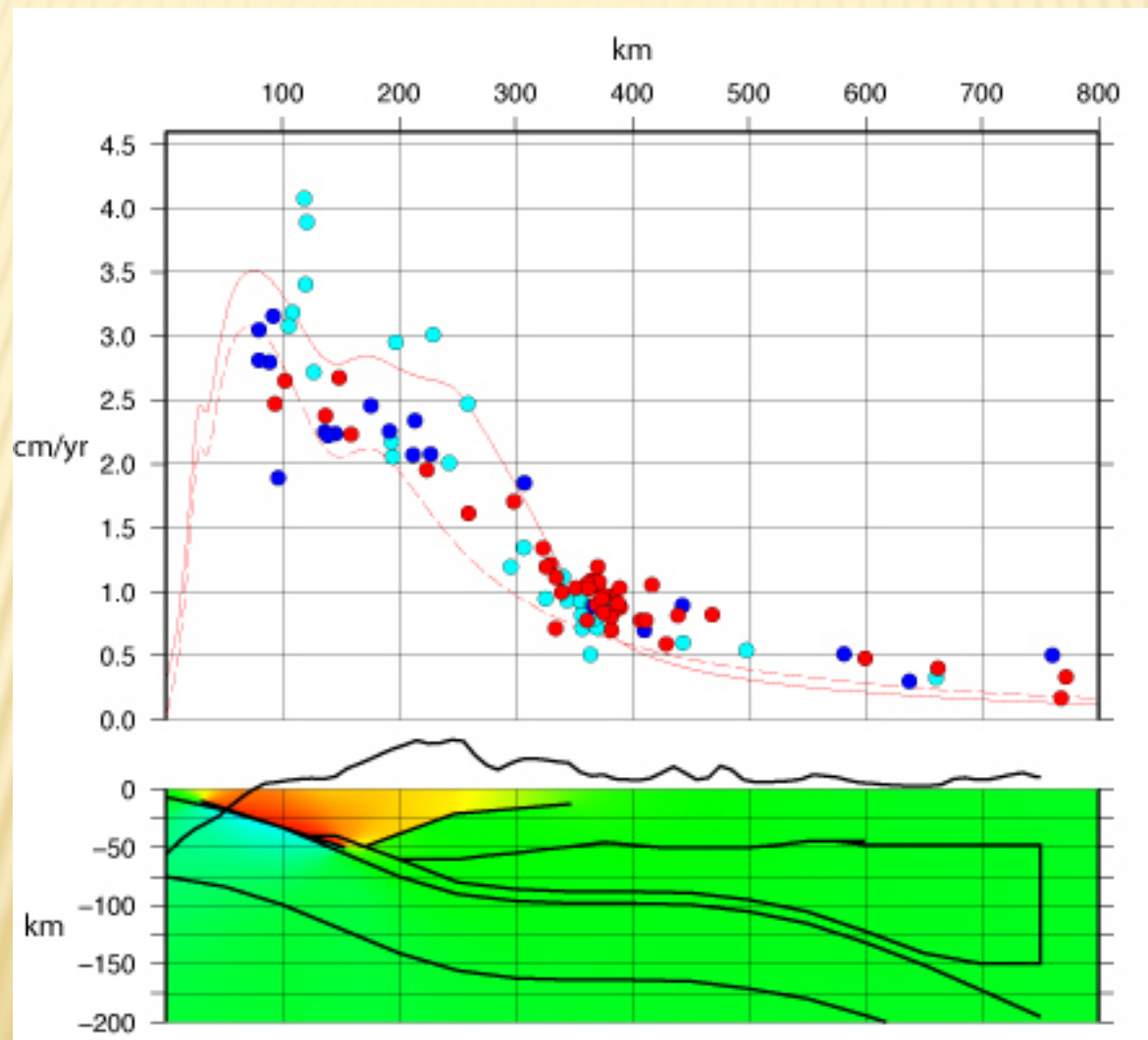
Add friction free fault representing decollement beneath thin-skinned thrust belt.



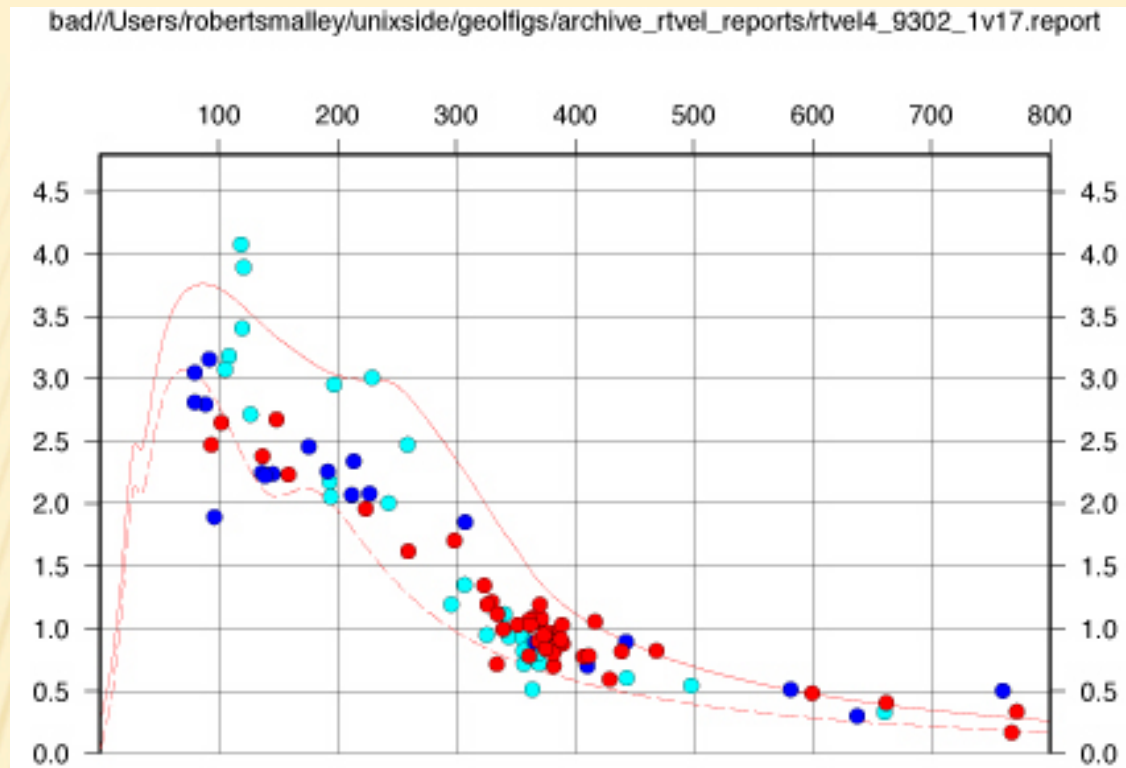
Add friction free fault representing decollement beneath thin-skinned thrust belt and “scoop” below main mountains (the dashed line geologists are wont to draw there) .



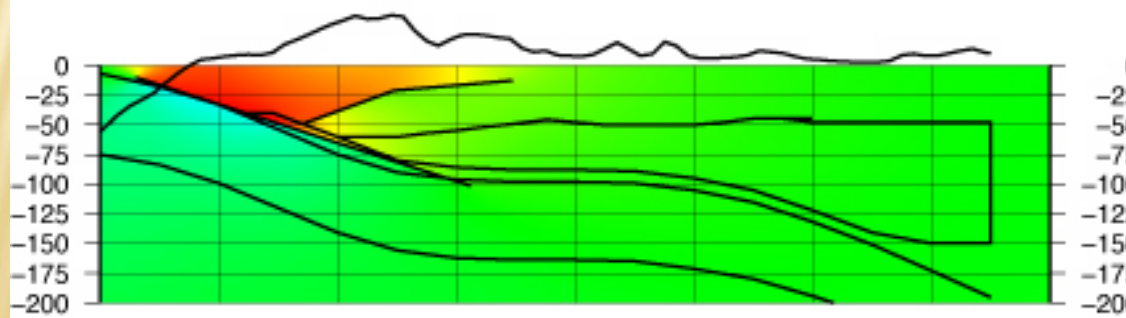
Send “scoop” all the way to the mocho/intersection with  
subducted plate..



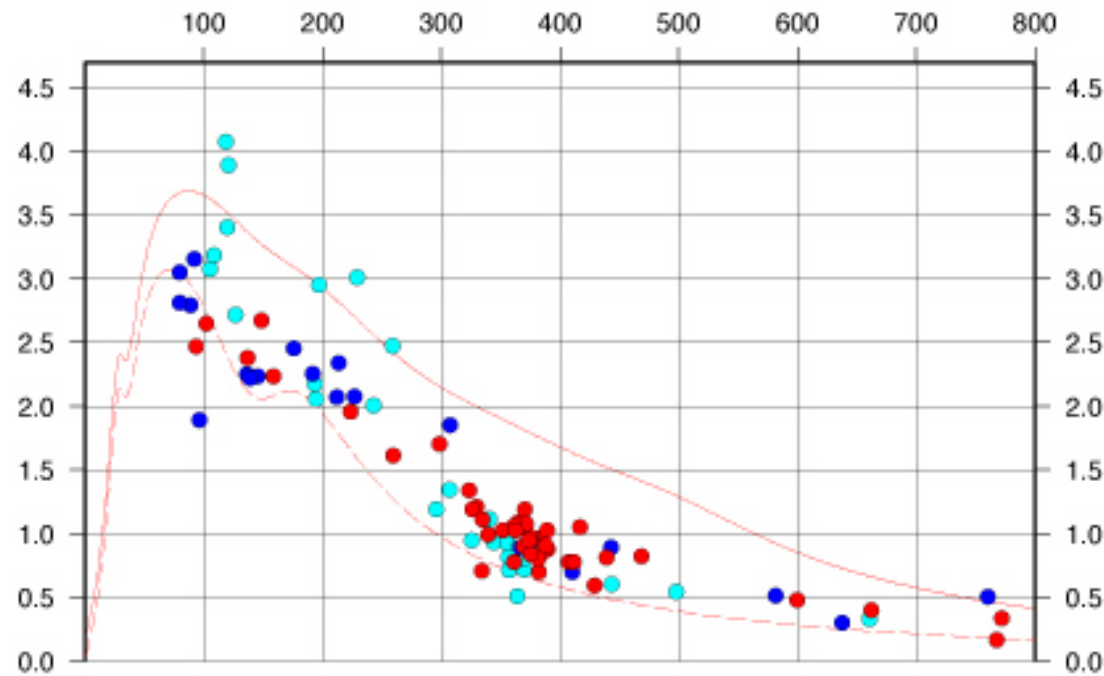




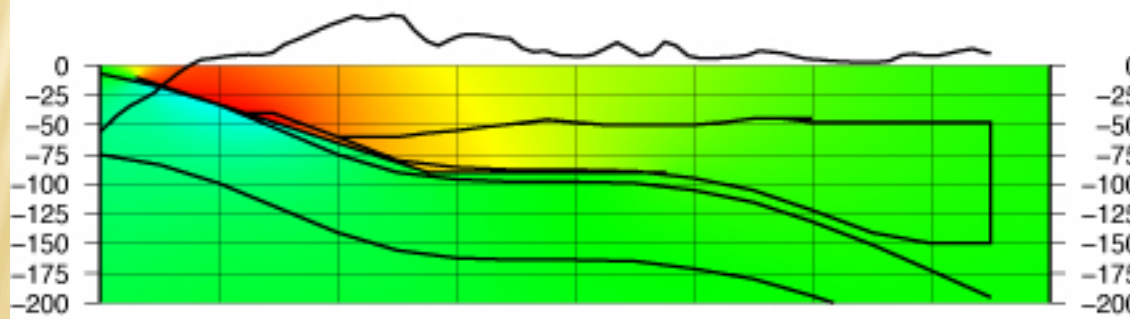
Add friction free extension of plate boundary.

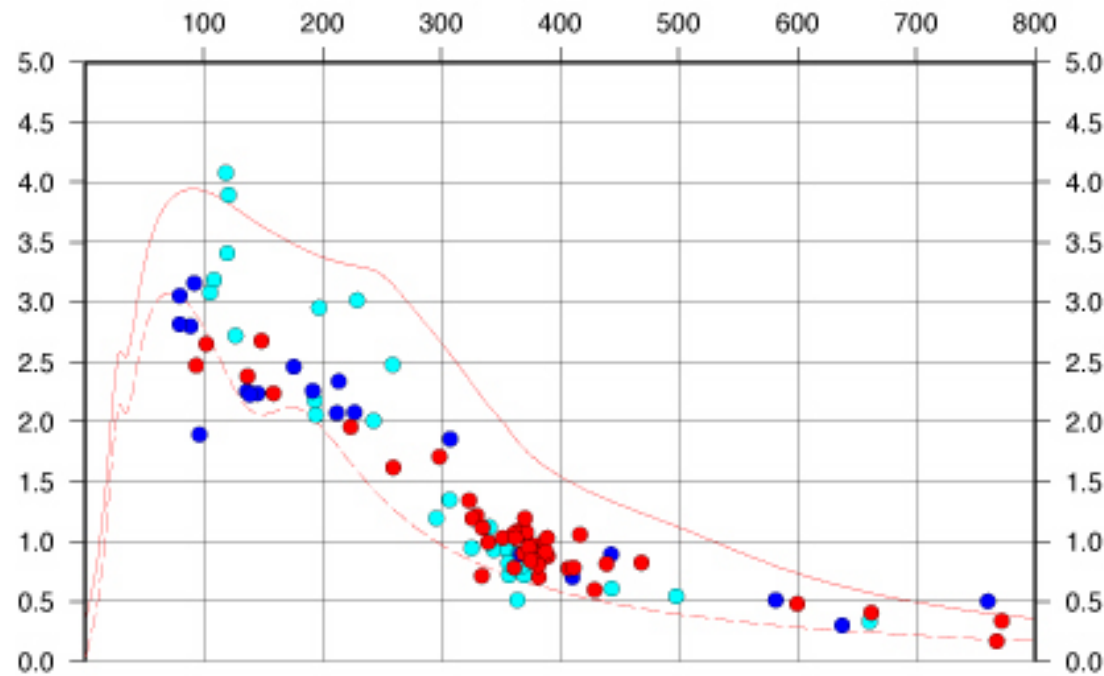




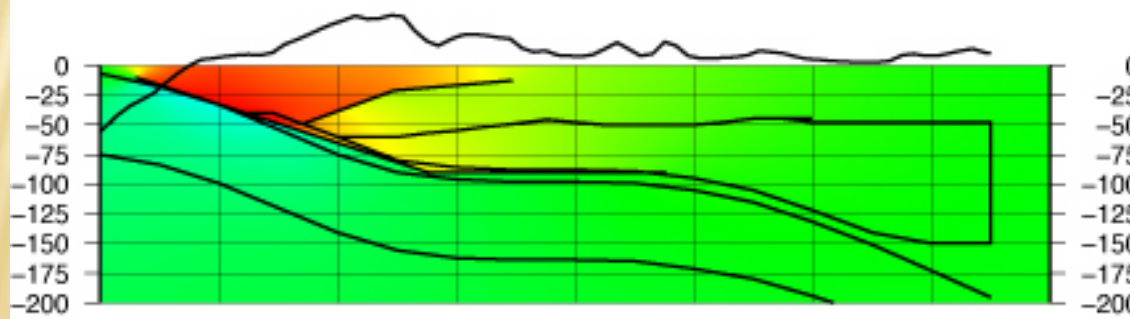


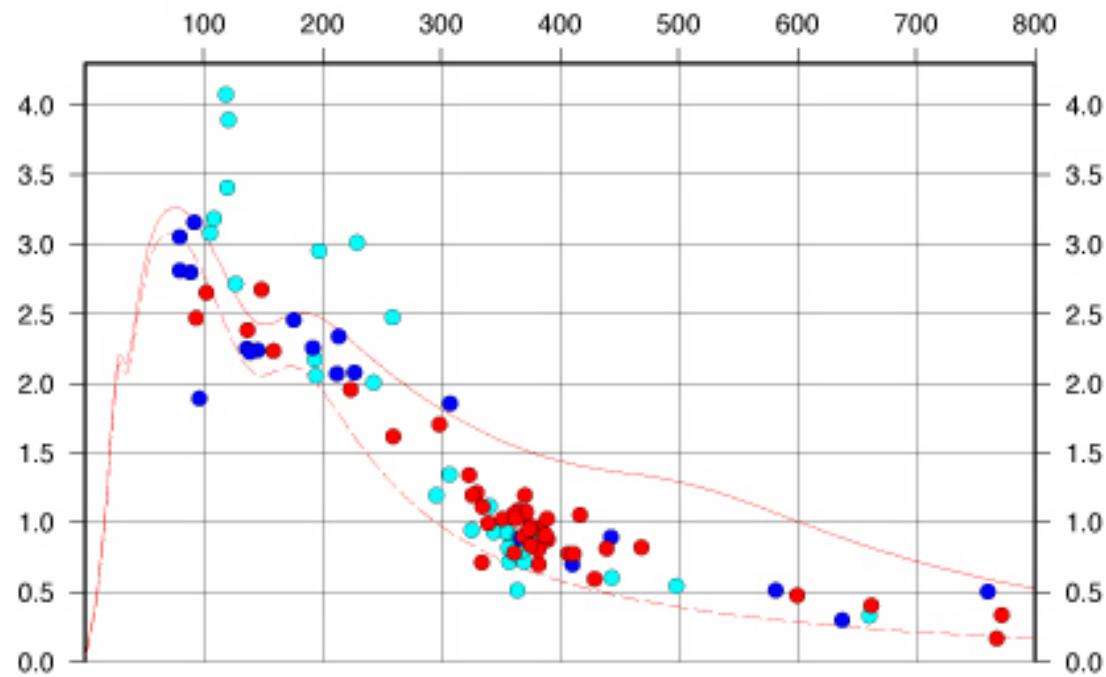
Add friction free extension of plate boundary and friction free base of upper lithosphere, not crustal structures.



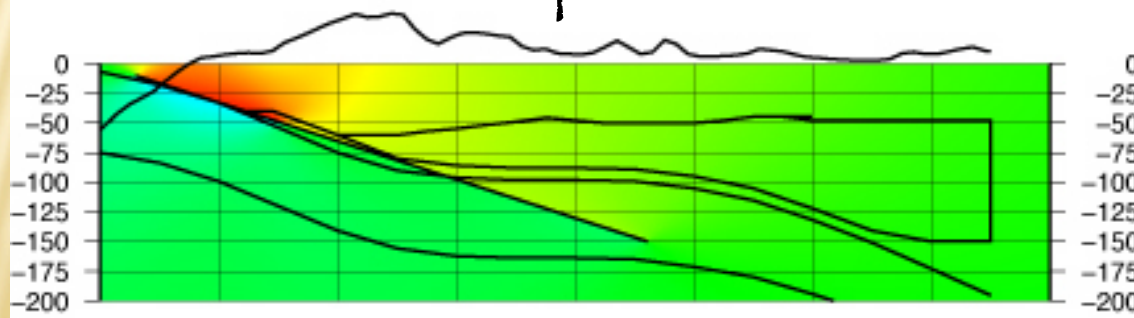


Friction free extension of plate boundary and friction free base of upper lithosphere, with crustal structures.

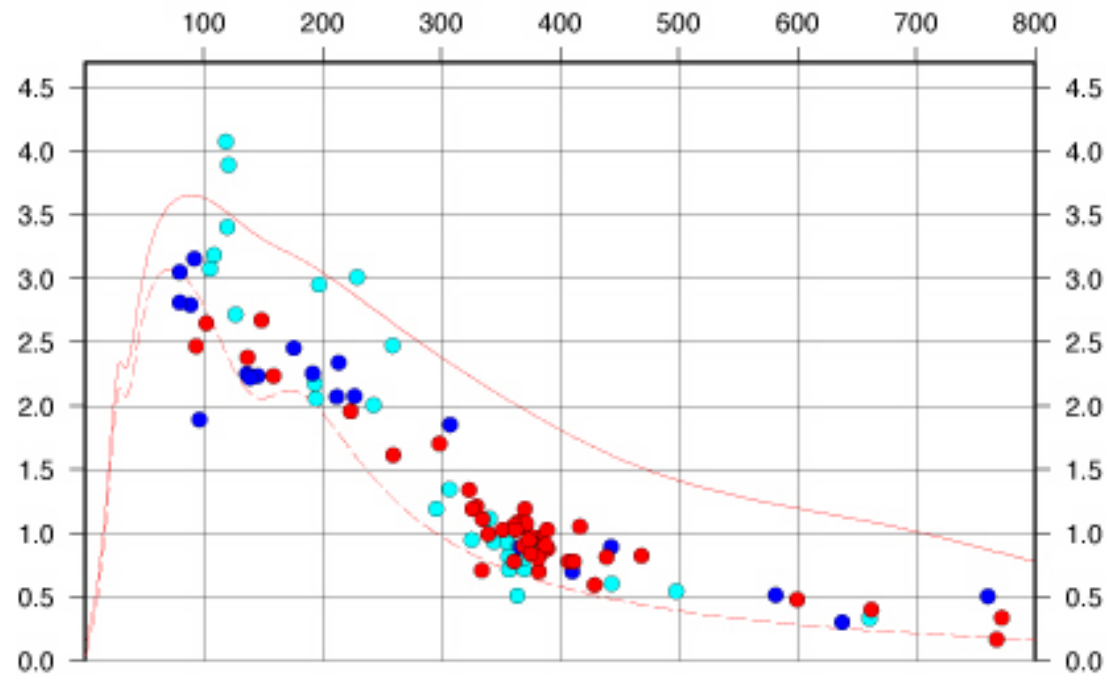




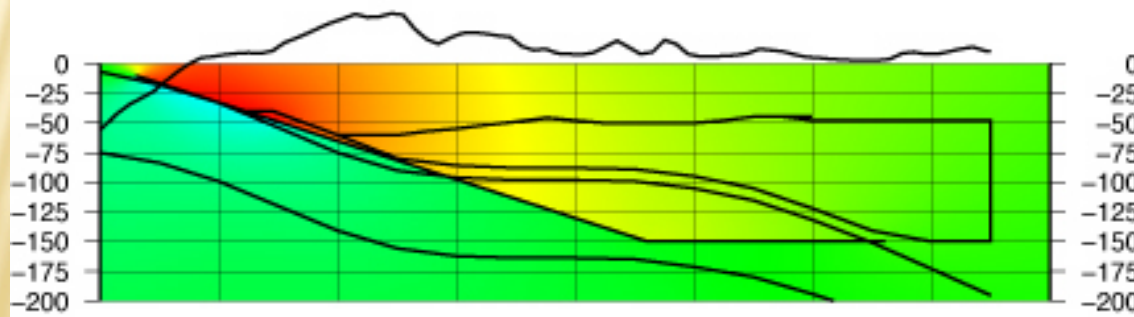
Friction free extension of plate boundary to 150 km depth.







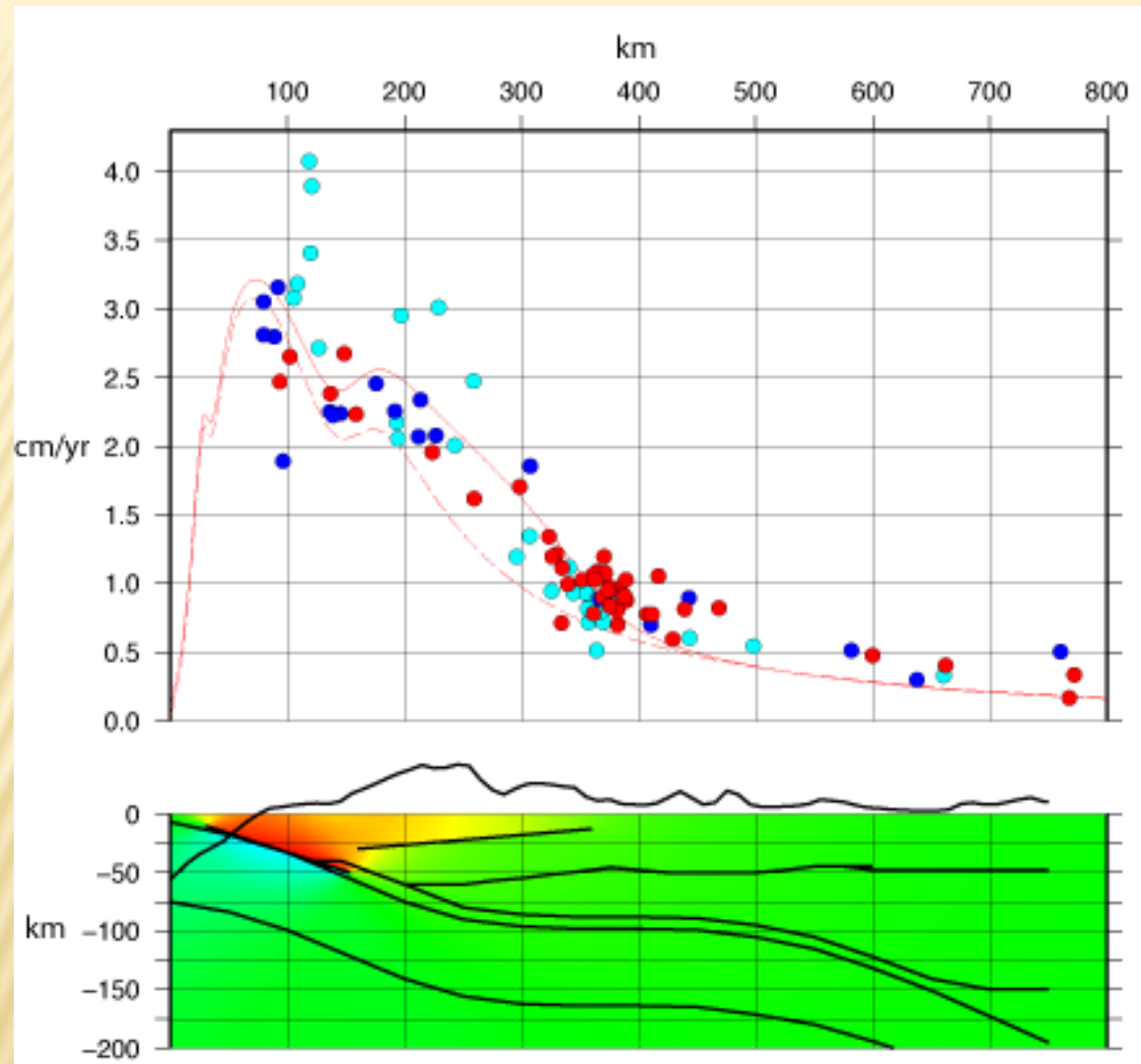
Friction free extension of plate boundary and friction free base of upper lithosphere at 150 km depth.





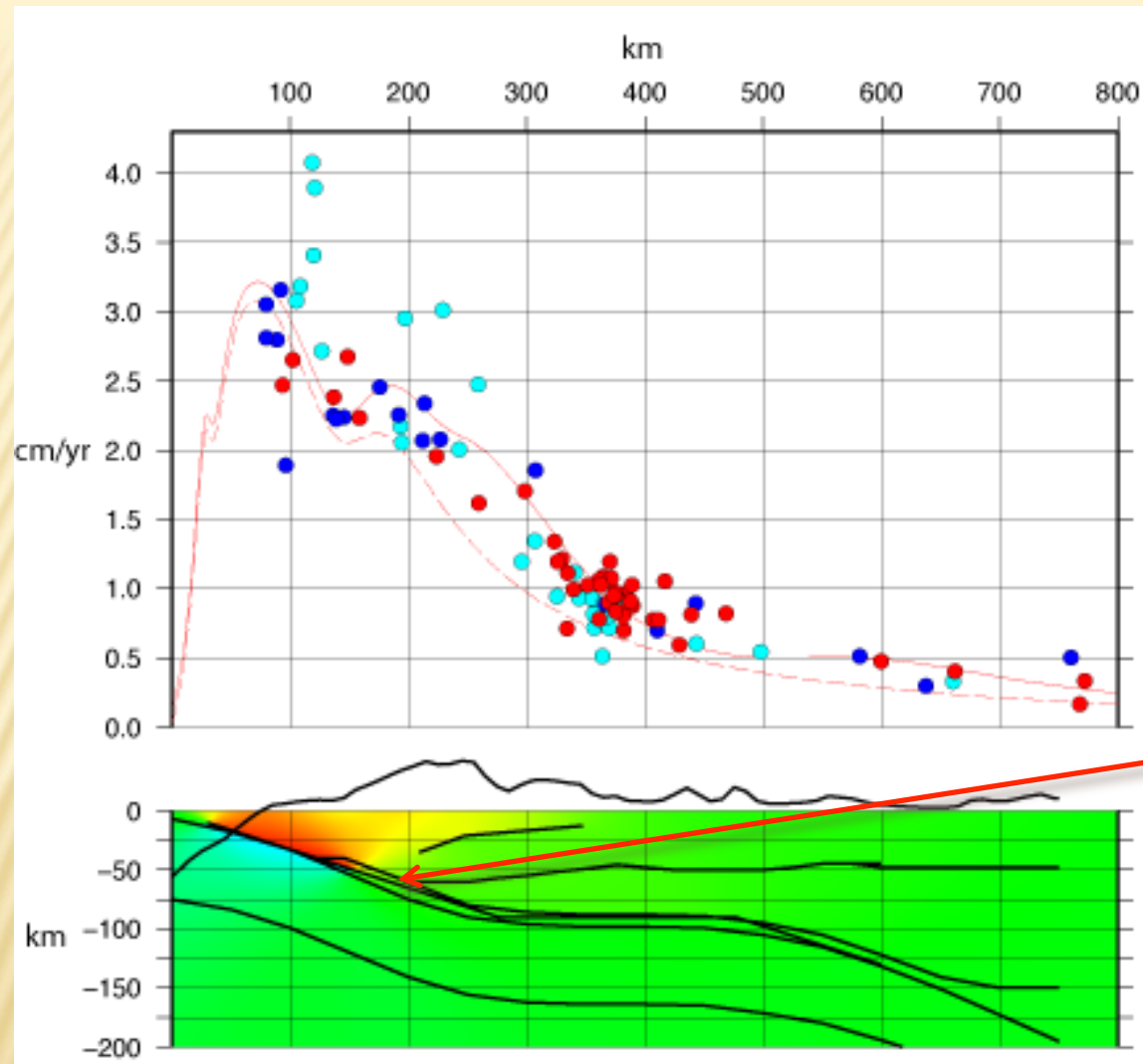
**Add freely  
slipping  
décollement in  
back arc crust.**

**“sucks-up”  
deformation into  
crust above  
décollement to  
match GPS data.**



**Horizontal  
displacement**

**Still too slow at  
greater  
distances.**



**Horizontal  
displacement**

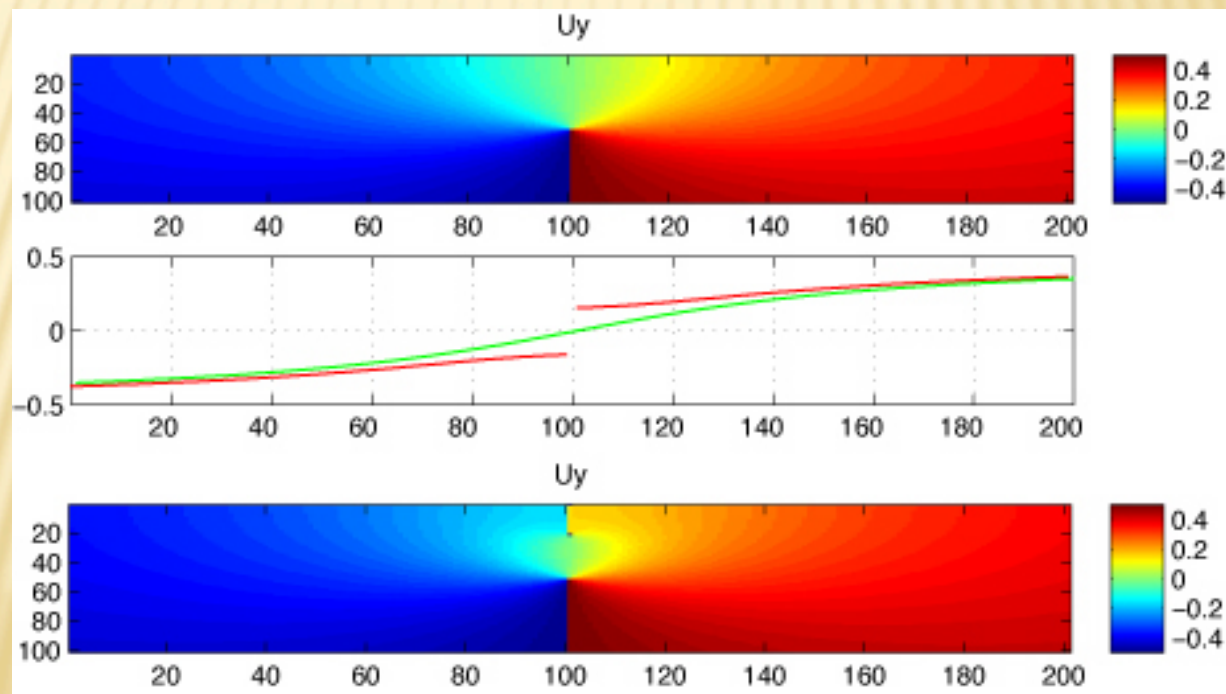
**Add “push” from  
relative plate  
convergence  
(normal force  
only on dipping  
plate interfaces  
at >50 km depth).**

**“throws”  
deformation to  
greater  
distances.**

Other popular variant.

Creeping section at surface on otherwise locked fault.

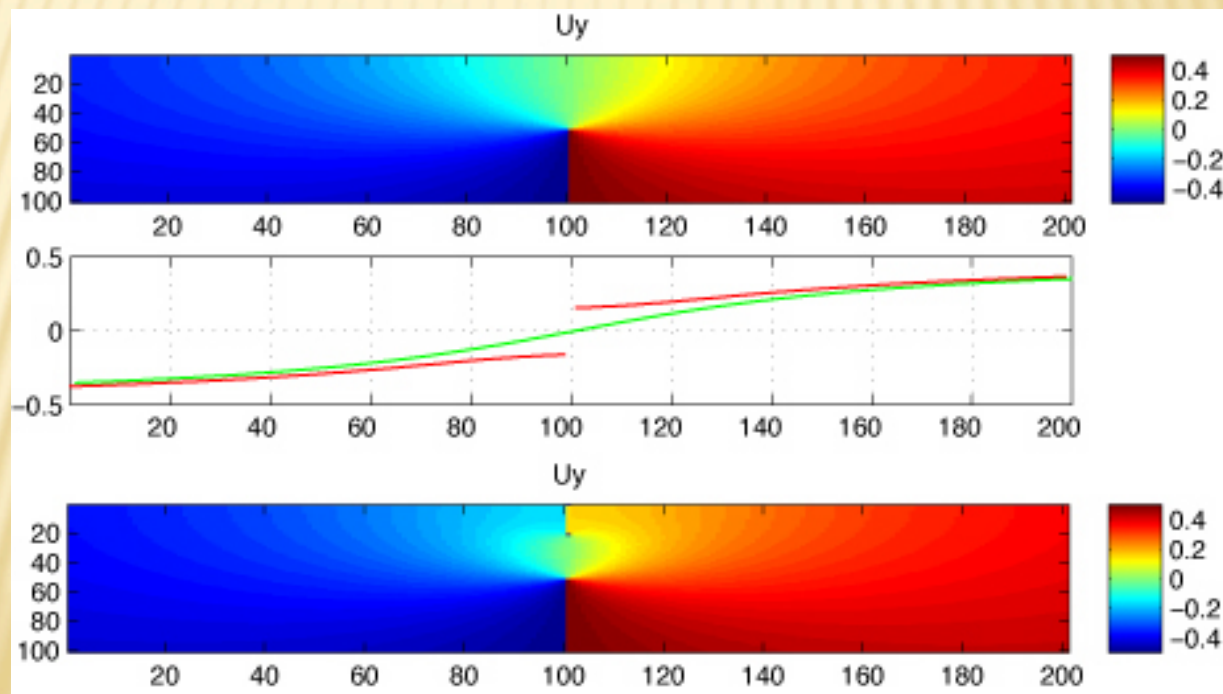
Can do it by putting in fault with specified slip, or in a self-consistent manner by putting in frictionless fault and letting it find equilibrium.





Use physically based model (slip on fault starting at locking depth and going to “infinity”) rather than backslip (top, green line), with friction free fault (bottom, red line).

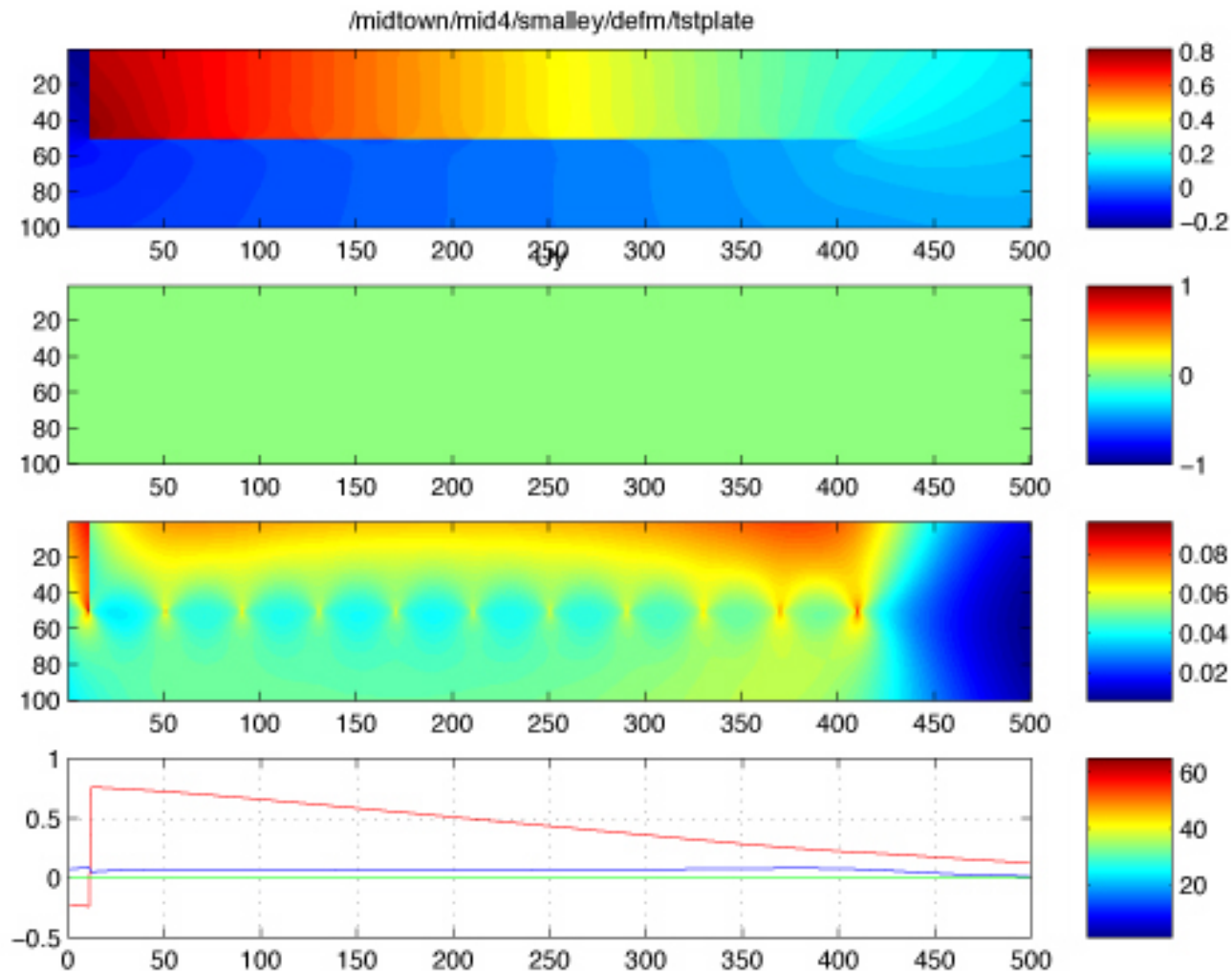
Now have offset across fault trace (from creep).



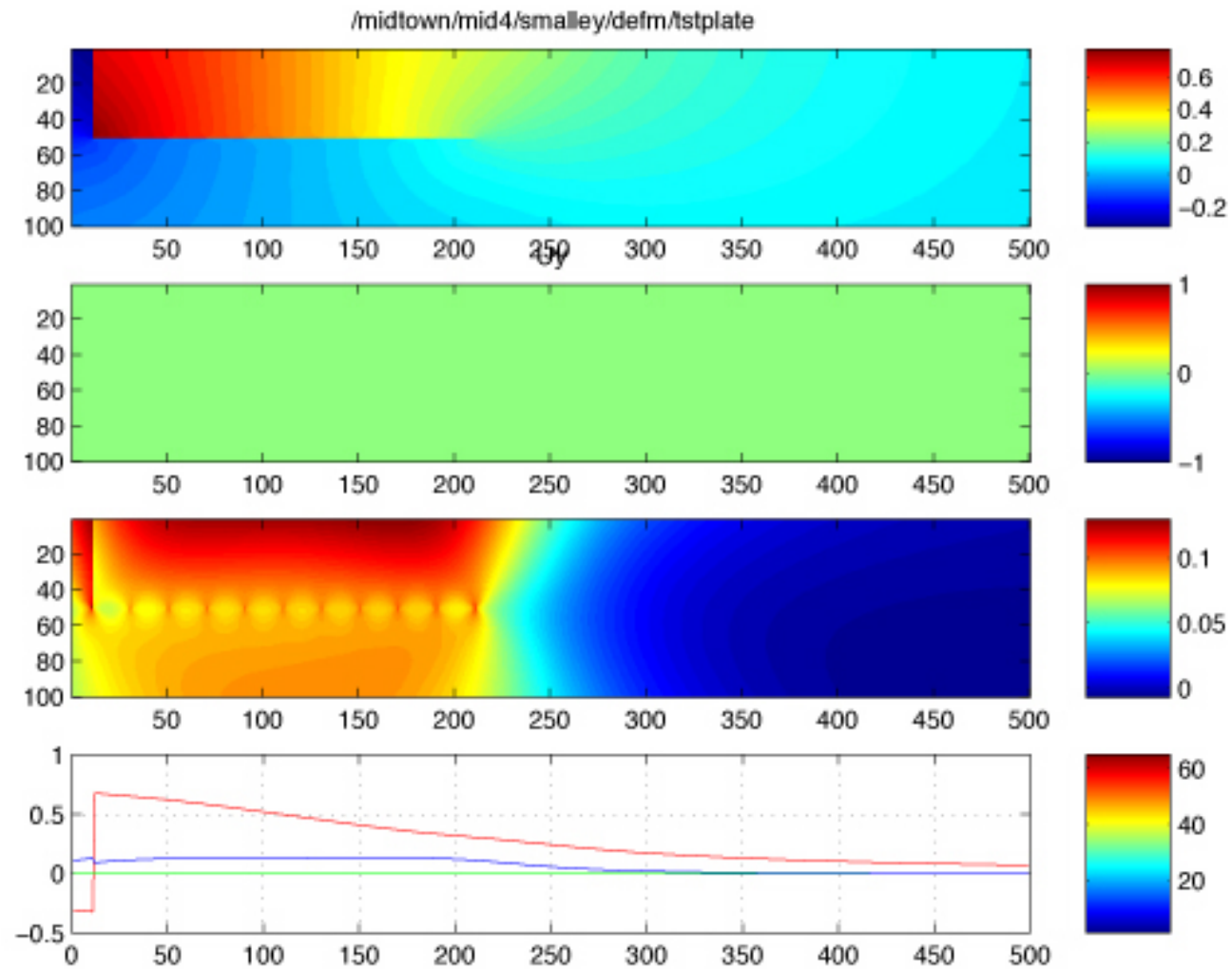


## Random Stuff:

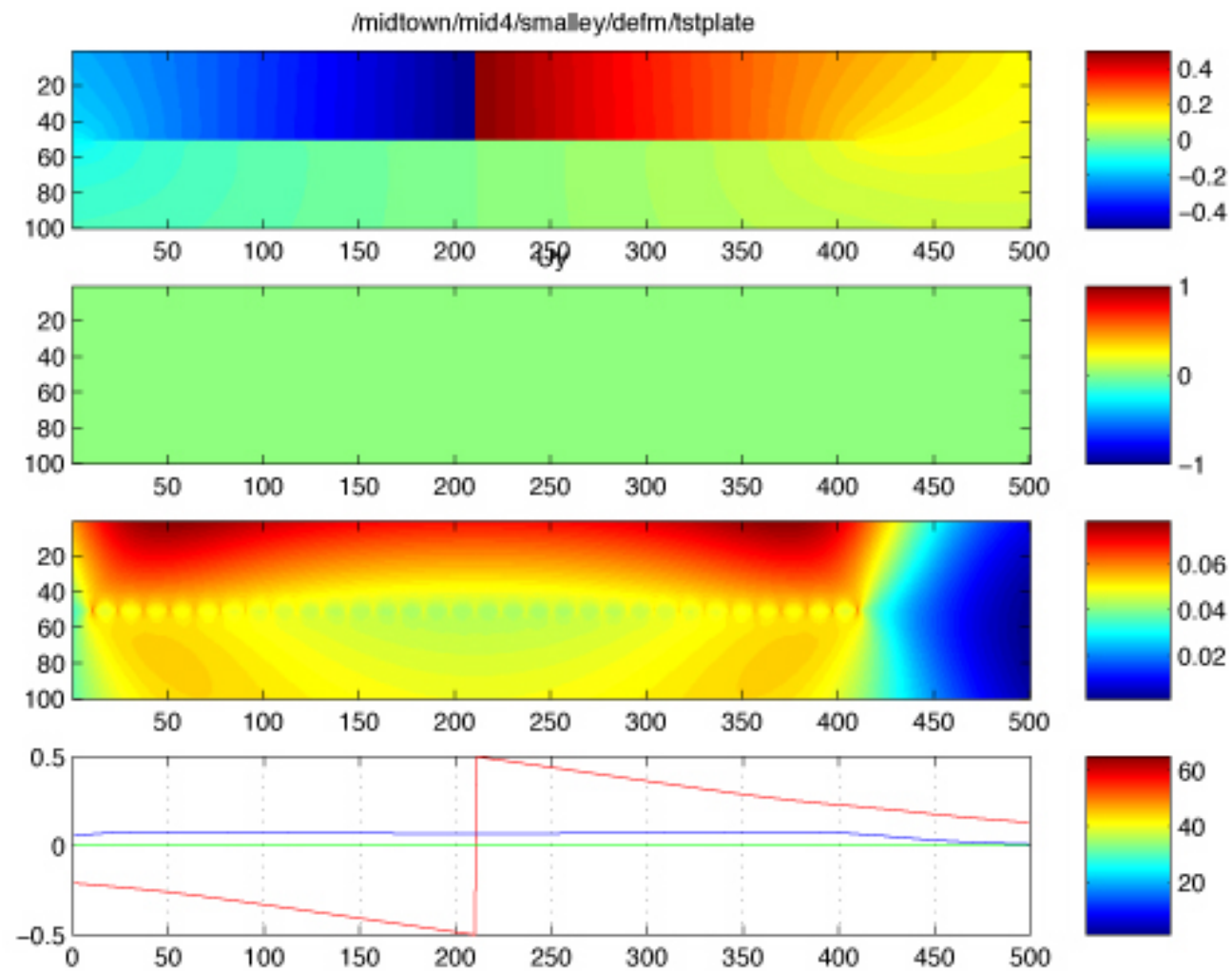
Simulate end loaded plate (right end not rigidly mounted). “smoothness” of result depends on number subelements.



# Smaller elements



# Push out

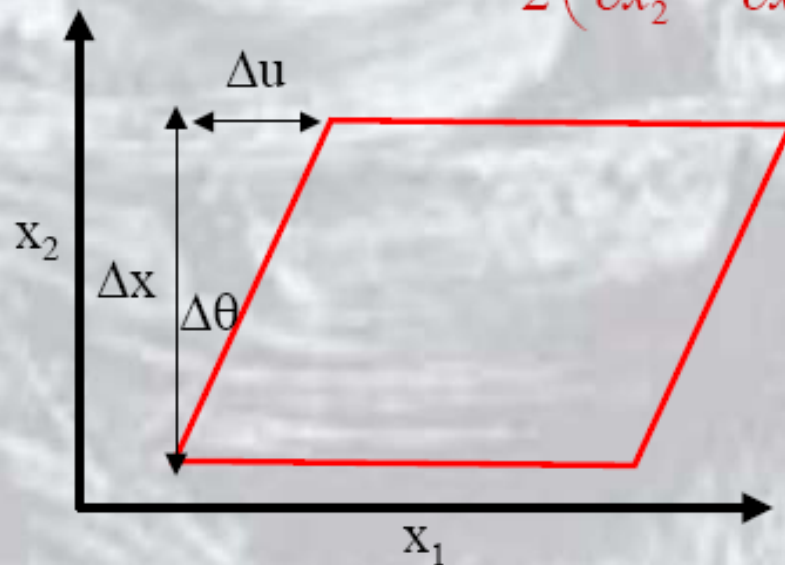


# Components of strain: simple shear

## ● Mixed strain and rotation - *simple shear*

$$\varepsilon_{12} = \frac{1}{2} \left( \frac{\partial u_1}{\partial x_2} + \frac{\partial u_2}{\partial x_1} \right) = \frac{\Delta\theta}{2}$$

$$\omega_{12} = \frac{1}{2} \left( \frac{\partial u_1}{\partial x_2} - \frac{\partial u_2}{\partial x_1} \right) = \frac{\Delta\theta}{2}$$



$$\varepsilon_{12} = 1/2 ( \Delta u_1 / \Delta x_2 + 0 ) = \Delta\theta/2$$

$$w_{12} = 1/2 ( \Delta u_1 / \Delta x_2 + 0 ) = \Delta\theta/2$$



# Strain rates

Now we have to consider the time taken for the displacement field  $\mathbf{u}(\mathbf{x})$  to develop. If this time interval  $\Delta t$  is known, we can instead use the define velocity field  $\mathbf{v}(\mathbf{x})$ , where

$$v_i = \frac{u_i}{\Delta t}$$

The development is identical, producing a velocity gradient tensor and the following strain-rate and rotation-rate tensor:

$$\dot{\varepsilon}_{ij} = \frac{1}{2} \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)$$

$$\dot{\omega}_{ij} = \frac{1}{2} \left( \frac{\partial v_i}{\partial x_j} - \frac{\partial v_j}{\partial x_i} \right)$$

The 'dot' is shorthand for  $\partial/\partial t$

## Using survey data

If the displacement gradient tensor  $D_{ij}$  were known, we could calculate the relative displacement  $\mathbf{u}$  between a pair of points separated by the vector  $\mathbf{x}$  by using the chain rule:

$$\begin{aligned}u_1 &= \frac{\partial u_1}{\partial x_1} x_1 + \frac{\partial u_1}{\partial x_2} x_2 \\&= D_{11} x_1 + D_{12} x_2\end{aligned}$$

and similarly  $u_2 = D_{21} x_1 + D_{22} x_2$

In surveys (satellite or terrestrial) we measure  $\mathbf{u}$  and  $\mathbf{x}$  and want to calculate  $D_{ij}$ . The same equations can be used to solve for the components  $D_{ij}$ .

## Using survey data

In 2-D, solving for the 4 independent components  $D_{ij}$  requires surveys of displacements between two pairs of points, e.g.

$\mathbf{u}^a(\mathbf{x}^a)$  and  $\mathbf{u}^b(\mathbf{x}^b)$  :

$$u_1^a = D_{11}x_1^a + D_{12}x_2^a$$

$$u_2^a = D_{21}x_1^a + D_{22}x_2^a$$

$$u_1^b = D_{11}x_1^b + D_{12}x_2^b$$

$$u_2^b = D_{21}x_1^b + D_{22}x_2^b$$

This is a set of 4 simultaneous equations in 4 unknowns. After solution the strain and rotation tensors can be obtained from  $D_{ij}$ .